

ME 308
MACHINE ELEMENTS II

CHAPTER 4

JOURNAL BEARINGS_2

(NO ROLLING ELEMENTS,
ONLY A SHAFT AND A HOLE AND SOME
LUBRICANT/OIL IN BETWEEN)

The performance parameter temperature increase (ΔT) is formulated as

in American units
$$\Delta T_{o_F} = \frac{0.103P}{\left[1 - \frac{1}{2} \times \frac{Q_s}{Q}\right]} \times \frac{\frac{r}{c} f}{rcNl}$$

in SI units
$$P \rightarrow \frac{lb}{in^2}, \quad Q \& Q_s \rightarrow \frac{in^3}{sec}, \quad r, c, l \rightarrow in \quad \text{etc.}$$

$$\Delta T_{o_c} = \frac{8.30P}{\left[1 - \frac{1}{2} \times \frac{Q_s}{Q}\right]} \times \frac{\frac{r}{c} f}{rcNl}$$

$$P \rightarrow \frac{MN}{m^2}, \quad Q \& Q_s \rightarrow \frac{m^3}{sec}, \quad r, c, l \rightarrow m \quad \text{etc.}$$

$$S = \left(\frac{r}{c}\right)^2 \frac{\mu N}{P}$$

or
$$\Delta T_{o_c} = T_{var} \frac{P}{\gamma C_H}$$

*** To be able to determine temp increase ΔT we need to know parameters:**

$$\frac{r}{c} f, \quad \frac{Q}{rcNl} \& \frac{Q_s}{Q} \quad \text{and} \quad T_{var}$$

and these parameters are dependent on S and hence on μ .

μ is also dependent on ΔT again !!

If you prefer using

$$\Delta T_{oc} = T_{var} \frac{P}{\gamma C_H}$$

where T_{var} is S dependent given in fig. 12.12

To be able to use a correct value of μ in S eqn.

$$S = \left(\frac{r}{c} \right)^2 \frac{\mu N}{P}$$

we need to know μ which is dependent on ΔT again

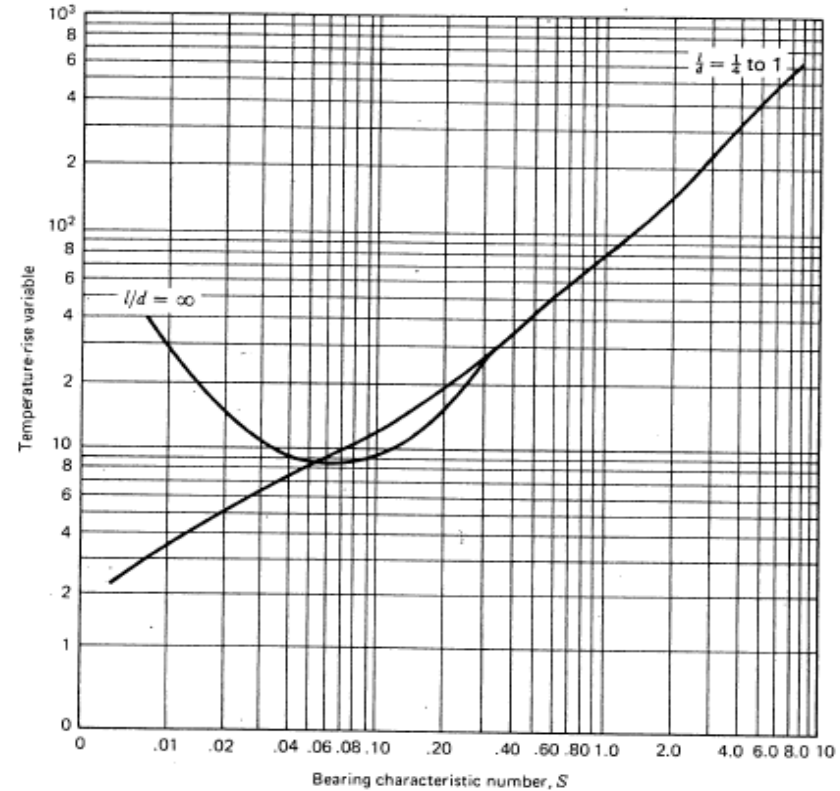


FIGURE 12-12 Chart for temperature-rise variable $T(\text{var}) = \gamma C_H \Delta T / P$. In plotting this chart it was found that the curves for $l/d = \frac{1}{4}, \frac{1}{2},$ and 1 were so close together that they could not be distinguished from a single curve.

Thus there is a situation where we need to start an assumption of either ΔT or μ and check whether the assumption is correct as in the case of tapered roller bearings ($K=1.5$) of TIMKEN.

There are two trial methods:

First one:

- 1) a) Assume a trial value for the temperature increase ($\Delta T = ?$)
- b) Calculate T_{ave} and determine μ from chart μ vs T_{ave}
- c) Calculate S and other related parameters
- d) Calculate ΔT_{new} and check if $\Delta T_{new} \cong \Delta T_{old}$; if so OK.
- e) if not re-assume ΔT to be between ΔT_{new} & ΔT_{old} and re-do the calculations from b to d until $\Delta T_{new} \cong \Delta T_{old}$

Second trial method is:

- 2) a) Assume a trial value for the viscosity ($\mu = ?$) and
- b) then calculate S and related parameters such as $\frac{r}{c} f, \frac{Q_s}{Q}$ etc.
- c) calculate temperature increase ΔT and average temperature
$$T_{ave} = T_{in} + \frac{\Delta T}{2}$$
- d) determine μ_{new} from μ vs T_{ave} chart.
- e) check if $\mu_{new} \cong \mu_{old}$; if so design is OK.
- f) if not re-assume μ to be between μ_{new} & μ_{old} and re-do the calculations from b to e until $\mu_{new} \cong \mu_{old}$

EXAMPLE 4.1

A sleeve bearing is 10 mm in diameter and 10 mm long. SAE 10 lubricating oil at an inlet temperature of 50° C is used to lubricate the bearing. The bearing is copper-lead alloy and the journal rotates at 3600 rpm. If the radial load on the bearing is 68 N. Find:

- a) temperature rise of the lubricant,
- b) the minimum oil-film thickness,
- c) the power loss in the bearing.
- d) oil flowrate-oil consumption

Given:

$l = 10 \text{ mm}$
 $d = 10 \text{ mm}$ } $\underline{l/d=1}$
 SAE 10 oil
 $T_i = 50^\circ \text{ C}$
 $T_o = ?$
 $T_{ave} = ?$
 bearing copper-lead
 $N = 3600 \text{ rev/min} = 60 \text{ rev/sec}$
 $W = 68 \text{ N}$

$\Delta T = ?$

Required:

$\Delta T = ? ^\circ \text{ C}$
 $h_o = ?$
 $P_{loss} = ?$

$$S = \left(\frac{r}{c}\right)^2 \frac{\mu N}{P}$$

\downarrow
 $\frac{W}{ld}$

S dependent

$$\Delta T_{oc} = \frac{8.30P}{\left[1 - \frac{1}{2} \times \frac{Q_s}{Q}\right]} \times \frac{\frac{r}{c} f}{\frac{Q}{rcNl}}$$

or

$$\Delta T_{oc} = T_{var} \frac{P}{\gamma C_H}$$

S is μ dependent

μ is T_{ave} dependent hence ΔT dependent.

a) So,

$$\Delta T \rightarrow S \rightarrow \mu \rightarrow T_{ave} \rightarrow \Delta T$$

There is a vicious circle of which the starting point can not be found. Now, we have to use trail and error method of assuming ΔT or μ

Let $\Delta T = 6^\circ\text{C}$

$$\Delta T_{oc} = T_{var} \frac{P}{\gamma C_H}$$

$$S = \left(\frac{r}{c}\right)^2 \frac{\mu N}{P}$$

Where c is unknown \rightarrow use Table 12.4

For Copper-lead
 $r/c = 500-1000$
 let $r/c = 600$;

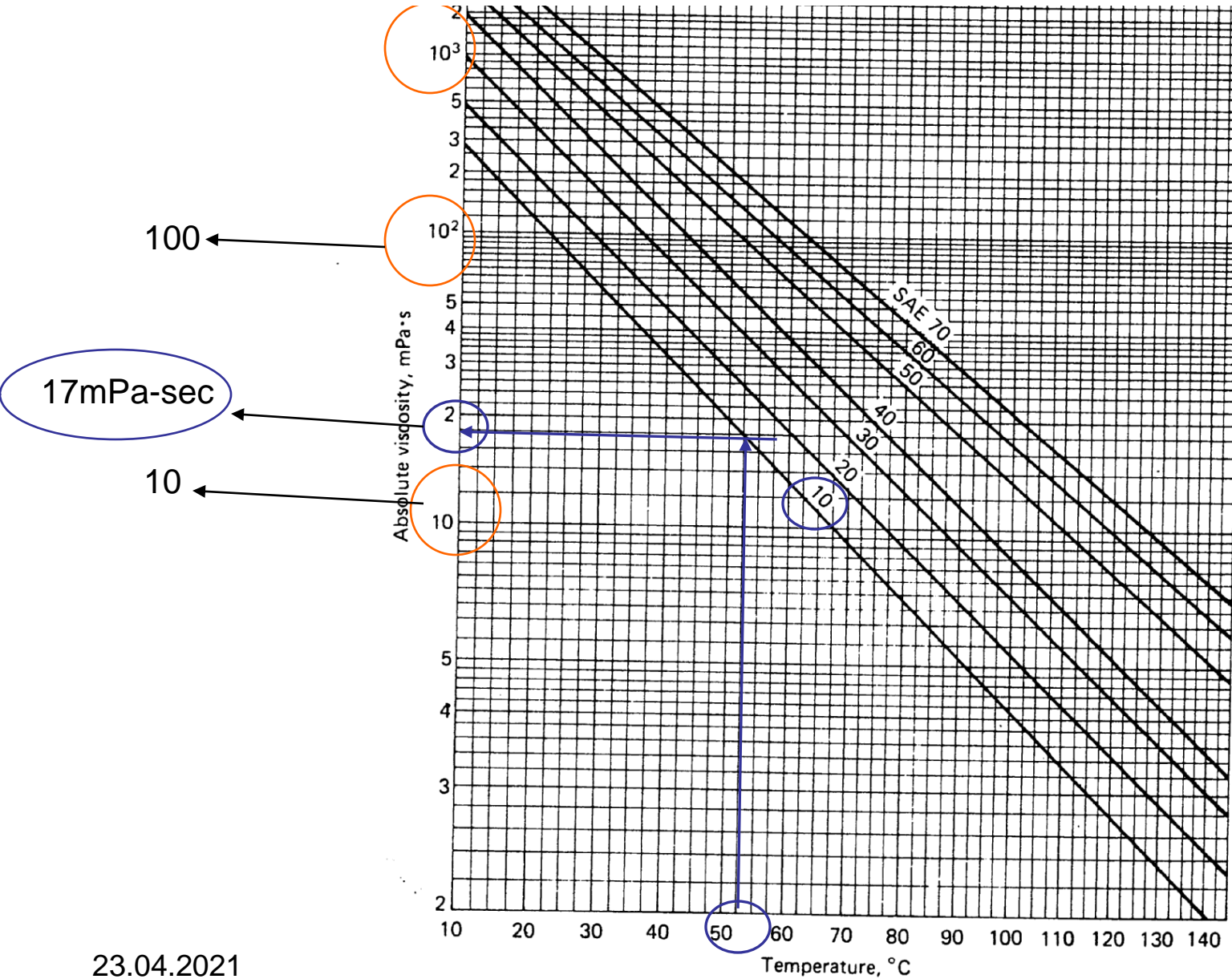
Table 12-4 SOME CHARACTERISTICS OF BEARING ALLOYS

Alloy name	Thickness, mm	Clearance ratio r/c	Load capacity	Corrosion resistance
Tin-base babbitt	0.559	600-1000	1.0	Excellent
Lead-base babbitt	0.559	600-1000	1.2	Very good
Tin-base babbitt	0.102	600-1000	1.5	Excellent
Leaded bronze	Solid	500-1000	3.3	Very good
Copper-lead	0.559	500-1000	1.9	Good
Aluminum alloy	Solid	400-500	3.0	Excellent
Silver plus overlay	0.330	600-1000	4.1	Excellent
Cadmium (1.5% Ni)	0.559	400-500	1.3	Good

$N = 60$ rev/sec given
 $P = W/(l*d) = 68\text{N}/(10\text{mm}*10\text{mm})$
 $P = 0.68\text{MPa} = 680\,000\text{Pa}$
 $\mu = ?$ At ave temp
 $T_{var} = ?$

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$$T_{ave} = T_{in} + \frac{\Delta T}{2} = 50 + 3 = 53 \text{ } ^\circ\text{C} \rightarrow \text{SAE } 10 \rightarrow \mu = 17 \text{ mPa} \cdot \text{sec}$$



23.04.2021

FIGURE 12-10 Viscosity-temperature chart.

So,

$$S = \left(\frac{r}{c}\right)^2 \frac{\mu N}{P} \quad S = (600)^2 \frac{(17 \times 10^{-3}) \times 60}{[68 / (0.01 \times 0.01)]} = (600)^2 \frac{0.017 \times 60}{680\,000 \text{ Pa}} = 0.54$$

$\mu \rightarrow \frac{W}{ld}$

Use S - T_{var} chart \longrightarrow for $S=0.54$ and $l/d=1$; $T_{var} = 47$

$$\Delta T = T_{var} \frac{P}{\gamma C_H} = 47 \frac{680\,000}{861 \times 1760} = 21 \text{ } ^\circ\text{C}$$

$$\Delta T_{ass} = 6 \text{ } ^\circ\text{C} < \Delta T_{calc} = 21 \text{ } ^\circ\text{C}$$

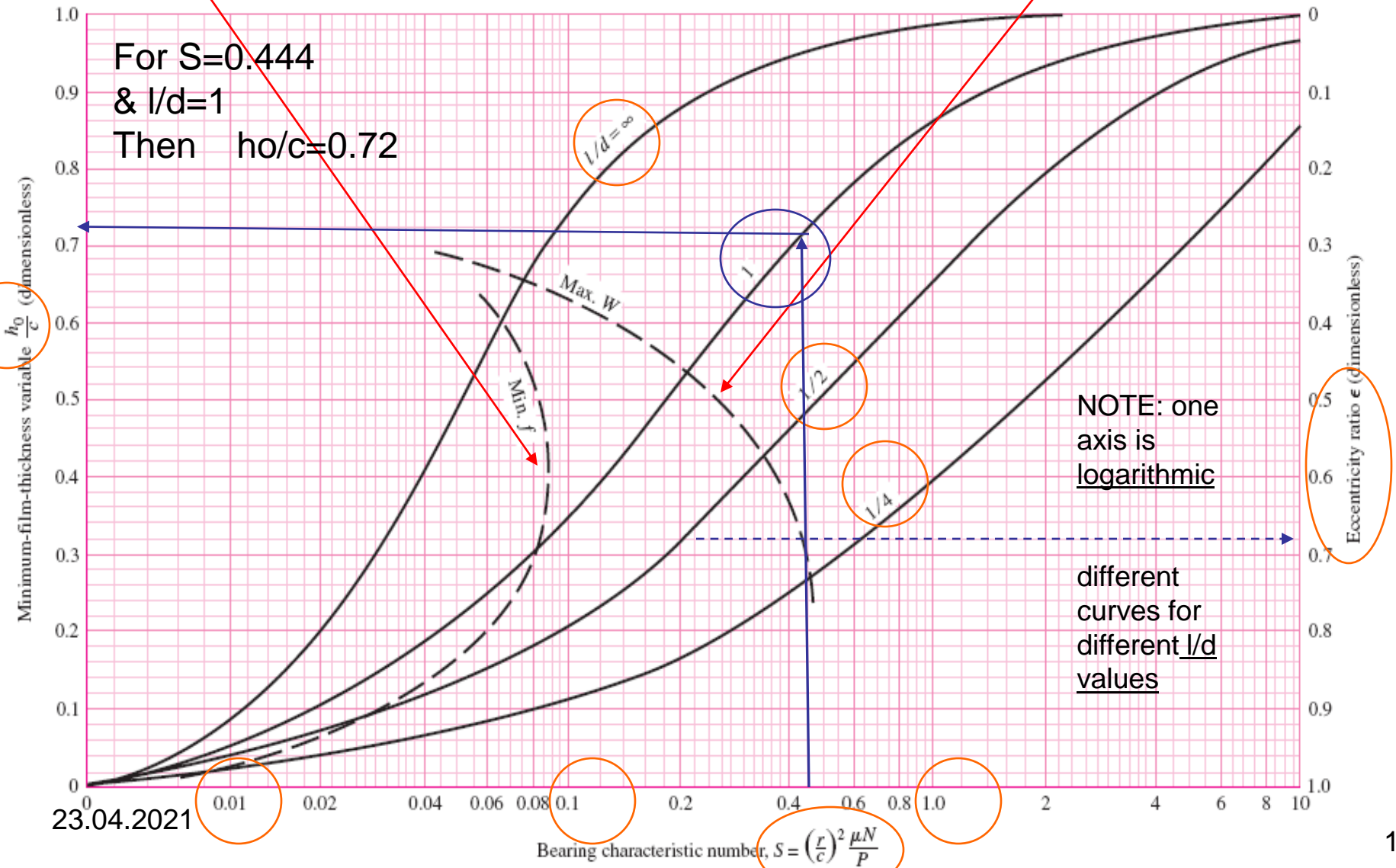
Let $\Delta T = 16 \text{ } ^\circ\text{C}$

$$T_{ave} = T_{in} + \frac{\Delta T}{2} = 50 + 8 = 58 \text{ } ^\circ\text{C} \rightarrow \text{SAE } 10 \rightarrow \mu = 14 \text{ mPa} \cdot \text{sec}$$

$$S = (600)^2 \frac{0.014 \times 60}{680\,000 \text{ Pa}} = 0.444 \longrightarrow T_{var} = 38 \text{ and } \Delta T = 17 \text{ } ^\circ\text{C}$$

$$\Delta T_{ass} \cong \Delta T_{calc} ; \quad \Delta T = 16 \text{ } ^\circ\text{C}$$

This is the chart for minimum film-thickness variable and eccentricity ratio.
 The left boundary (hidden line) of the zone defines the optimal h_0 for minimum friction; the right boundary is optimum h_0 for max. Load capacity.



$$b) h_o = ? \quad h_o / c = ?$$

$$S = 0.444 \rightarrow \frac{h_o}{c} = 0.72 \quad h_o = 0.72c$$

$$\frac{r}{c} = 600 \rightarrow c = \frac{r}{600} = \frac{5}{600} = 0.0083 \quad h_o = 0.72 \times 0.0083 = \underline{\underline{6 \mu m}}$$

$$c) \quad P_{loss} = T_{loss} \times \omega \frac{rad}{sec} \quad T_{loss} = F_{fric} \times r \quad F_{fric} = W \times f$$

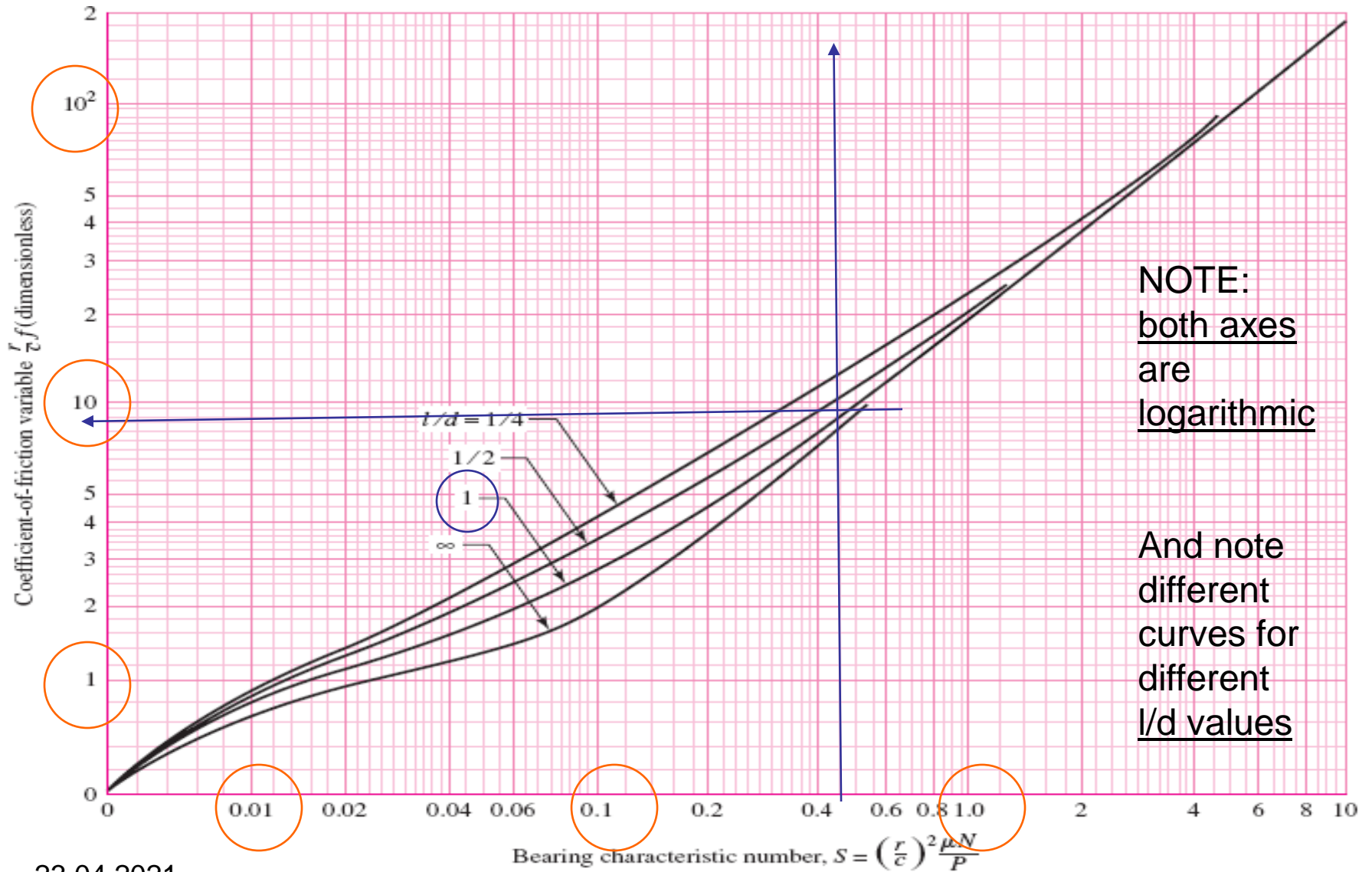
$$S = 0.444; \quad \frac{r}{c} f = 9.3 \rightarrow f = 0.0155$$

$$F_{fric} = 68 \times 0.0155 = 1.054 \text{ N}$$

$$T_{loss} = 1.054 \times 0.005 = 5.27 \times 10^{-3} \text{ Nm}$$

$$P_{loss} = 5.27 \times 10^{-3} \times 3600 \frac{rev}{min} \times \frac{2\pi rad}{rev} \times \frac{min}{60 sec} = 1.986 \text{ watt}$$

This is the chart for coefficient-of-friction variable;



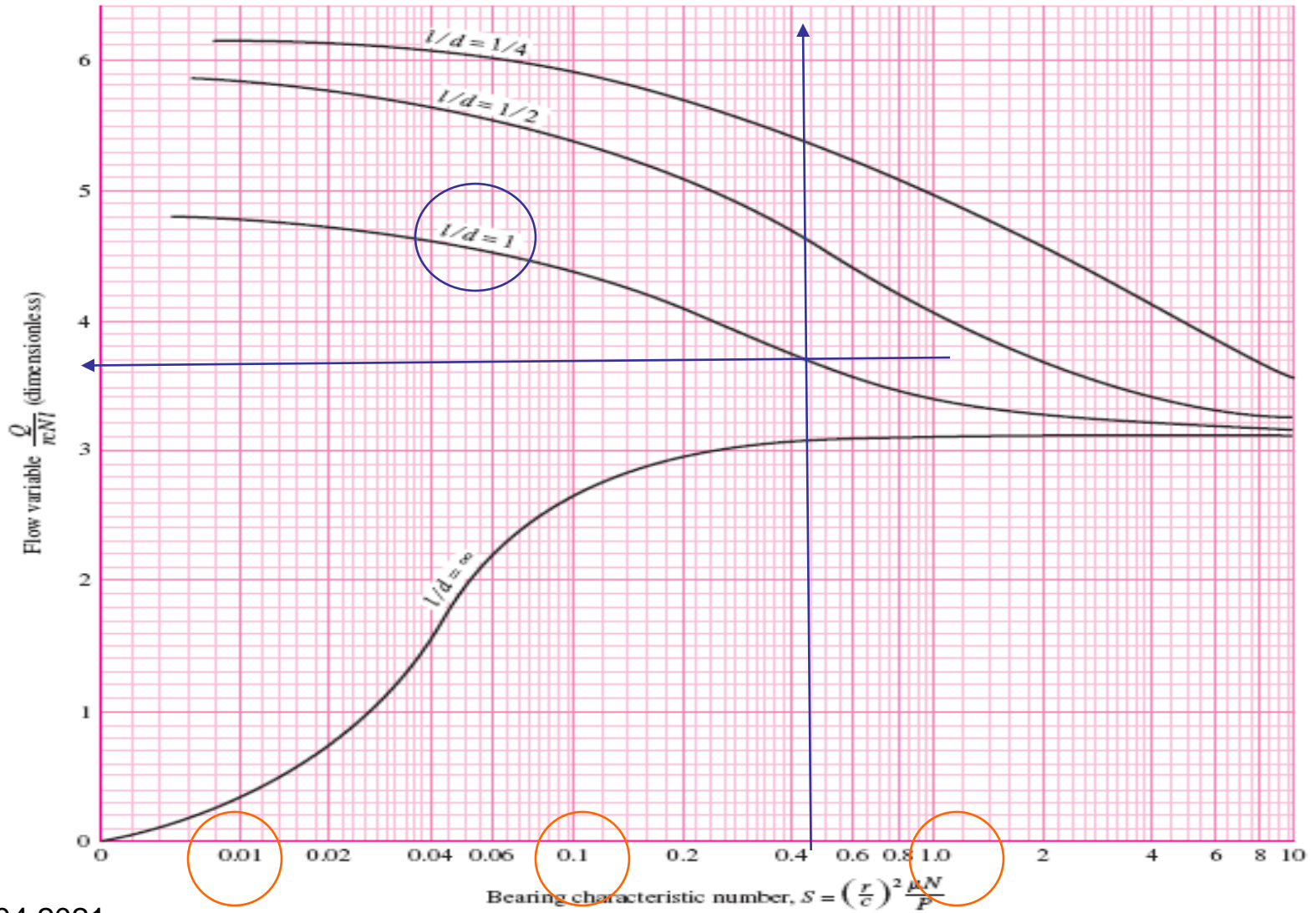
NOTE:
both axes
 are
logarithmic

And note
 different
 curves for
 different
 l/d values

- Oil flowrate Q is determined from charts again:
- $Q/rcNI$ vs S graph will help to determine Q
- From Chart $Q/rcNI=??$
- $Q=??*rcNI= \dots mm^3/sec = \dots lt/min = \dots kg/hr$

This is the chart for flow variable.

Note: Not to be used for pressure-fed bearings.



EXAMPLE 4.2

An 80 mm diameter full bearing on an air compressor is to be designed for a load of 6,6 kN, $N = 300$ rpm. It is desired that the bearing operates at a reasonable steady-state temperature (average temperature) of $50\text{ }^\circ\text{C}$. The journal is ground and operates in reamed-cast-bronze bearing.

- Compute all parameters of the bearing ($d, l, c, h_0, f, P_{max}, Q, Q_S, \Delta T$)
- Specify the oil to be used (SAE ??)
- Compute the amount of power loss in the bearing

SOLUTION:

GIVEN:

$D = 80\text{ mm}$

$W = 6,6\text{ kN}$

$N = 600\text{ rpm} = 300/60 = 5\text{ rps}$

$T_{ave} = 50\text{ }^\circ\text{C}$

Ground journal

Reamed-cast-bronze bearing

Air compressor

$$S = \left(\frac{r}{c} \right)^2 \frac{\mu N}{P}$$

S is the main parameter to determine all other parameters.

S requires

r, N, P, c and μ

$r = d/2 = 40\text{ mm}$

$N = 5\text{ rps}$

Others (P, c and μ) are not given or known

1) Since application type is known then P can be limited in table 12-3

$P = 1\text{--}2$ MPa for air compressor main bearings

$$P = \frac{W}{l \times d}$$

$$l = \frac{W}{P \times d} = \frac{6600}{1 \times 10^6 \times 0.08} = 0.0825$$

$$l = 82.5 \text{ mm}$$

For $d = 80$ mm $l = 80$ mm $P = \frac{W}{ld}$

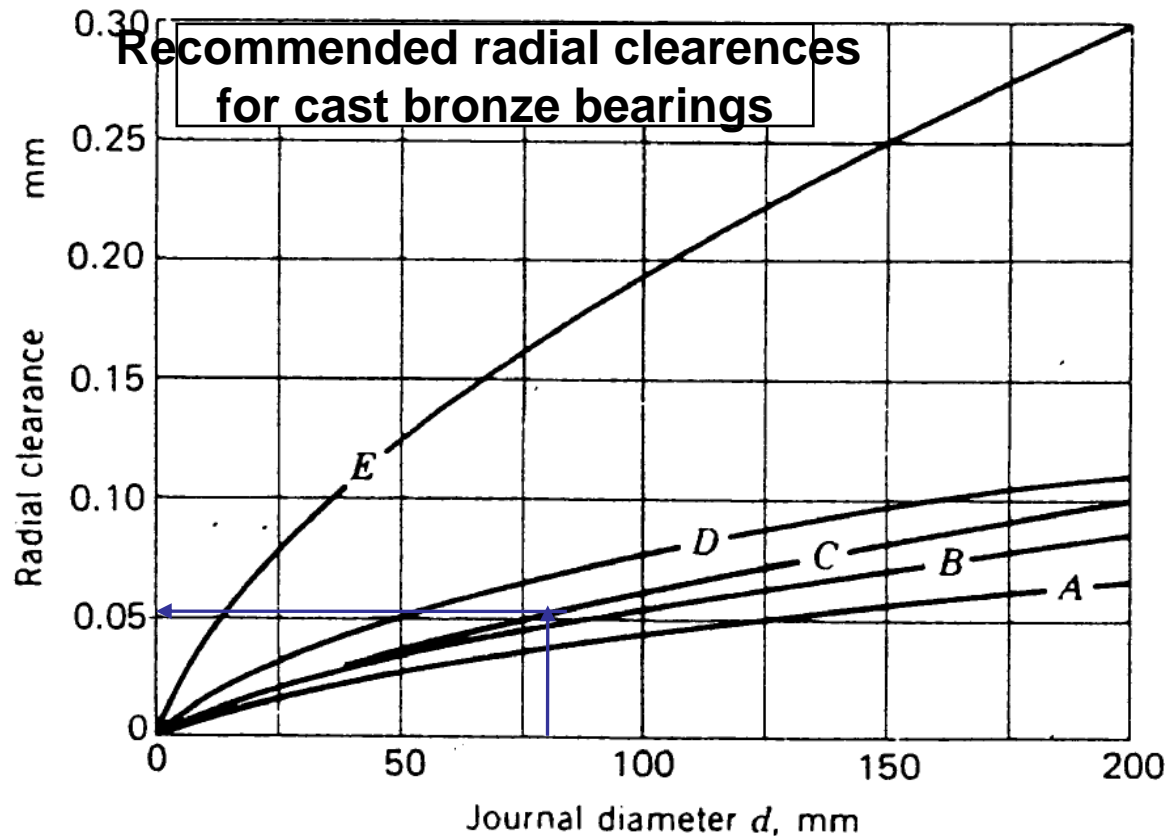
$$P = \frac{6600}{80 \times 80} = 1.031 \text{ MPa} \quad (\text{in the range OK})$$

Thus $\frac{l}{d} = \frac{80}{80} = 1$

Table 12-3 RECOMMENDED UNIT LOADS FOR SLEEVE BEARINGS

Application	Unit load, kPa	Application	Unit load, kPa
Air compressors:		Diesel engines:	
Main bearings	1 000– 2 000	Main bearings	6 000–12 000
Crankpin	2 000– 4 000	Crankpin	8 000–15 000
Automotive engines:		Wristpin	14 000–15 000
Main bearings	4 000– 5 000	Electric motors	800– 1 500
Crankpin	10 000–15 000	Gear reducers	800– 1 500
Centrifugal pumps	600– 1 200	Steam turbines	800– 1 500

2) Since bearing type is known the clearance value can be determined from Fig.12.29 pp.559 **curve C**. (Fig.12.27 pp.458 curve C.) **for ground journal and reamed cast-bronze bearing**



- All parameters of the bearing $h_0, f, P_{max}, Q, Q_S, \Delta T$ depends on S value
- S is the main parameter to determine all other parameters.

$$S = \left(\frac{r}{c} \right)^2 \frac{\mu N}{P}$$

S requires viscosity μ

Viscosity μ requires oil type

But oil type is unknown

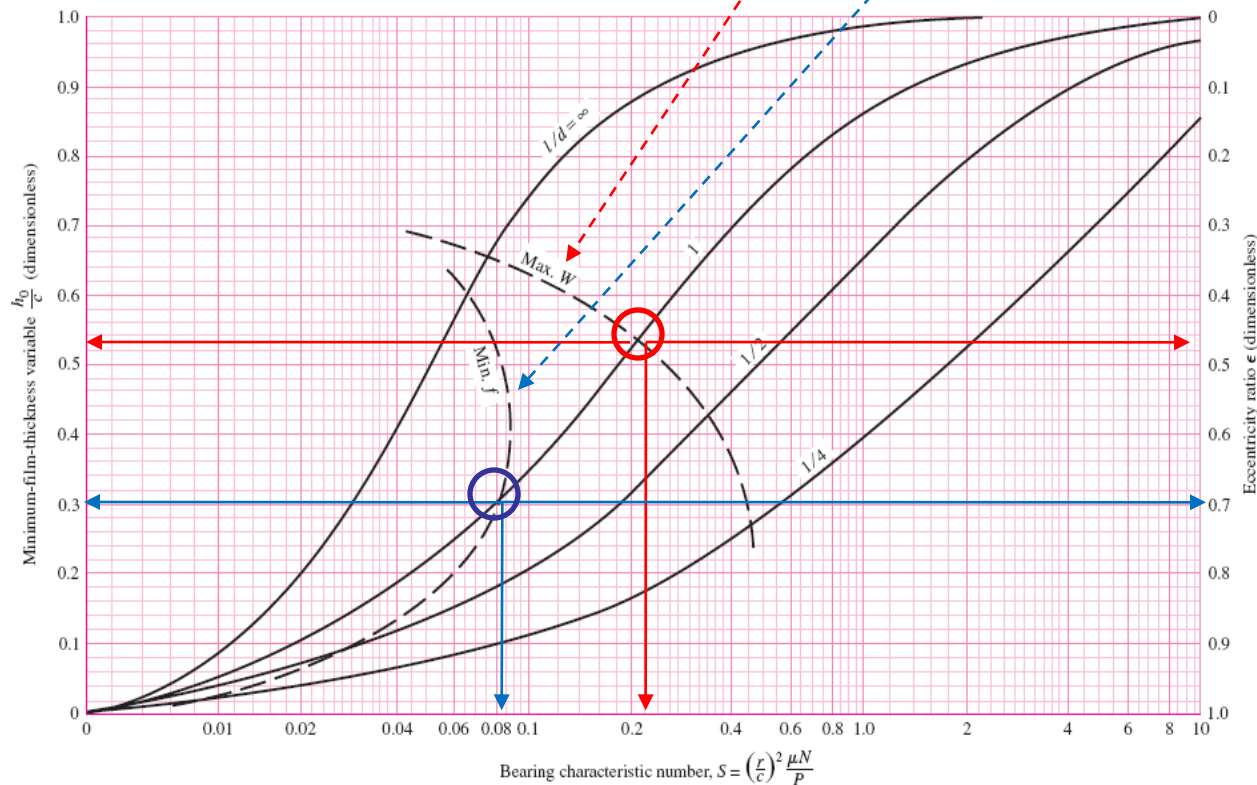
That means S can not be determined from the currently given parameters

Now we have the option of designing bearing based on two criteria

- Either for max load carrying capacity
- Or for minimum friction hence minimum power loss condition

3--> Now since $\frac{l}{d} = 1$ and $c = 0.05 \text{ mm}$

And none of the parameters are known we will make use of chart (f.12.14) of $\frac{h_0}{c}$ vs S for maximum load carrying capacity cond. and for min friction cond.



For max. W

$$\frac{h_0}{c} = 0.53$$

$$S = 0.21$$

$$\epsilon = 0.47$$

For min. f

$$\frac{h_0}{c} = 0.3$$

$$S = 0.08$$

$$\epsilon = 0.7$$

4) Since

$$S = \left(\frac{r}{c}\right)^2 \frac{\mu N}{P} = 0.21$$

Thus for max load capacity condition

$$\mu = \frac{S \times P}{N} \left(\frac{c}{r}\right)^2 = \frac{0.21 \times 1.031 \times 10^6}{5} \left(\frac{0.05}{40}\right)^2 = 0.0676 \text{ Pa} - \text{sec}$$

$$\mu = 67.6 \text{ mPa} - \text{sec}$$

again for min friction condition

$$S = \left(\frac{r}{c}\right)^2 \frac{\mu N}{P} = 0.08$$

$$\mu = \frac{S \times P}{N} \left(\frac{c}{r}\right)^2 = \frac{0.08 \times 1.031 \times 10^6}{5} \left(\frac{0.05}{40}\right)^2$$

$$\mu = 25.75 \text{ mPa} - \text{sec}$$

5) Now from chart Fig. 12.12 pp. 534 (Fig. 12.10 pp. 435)

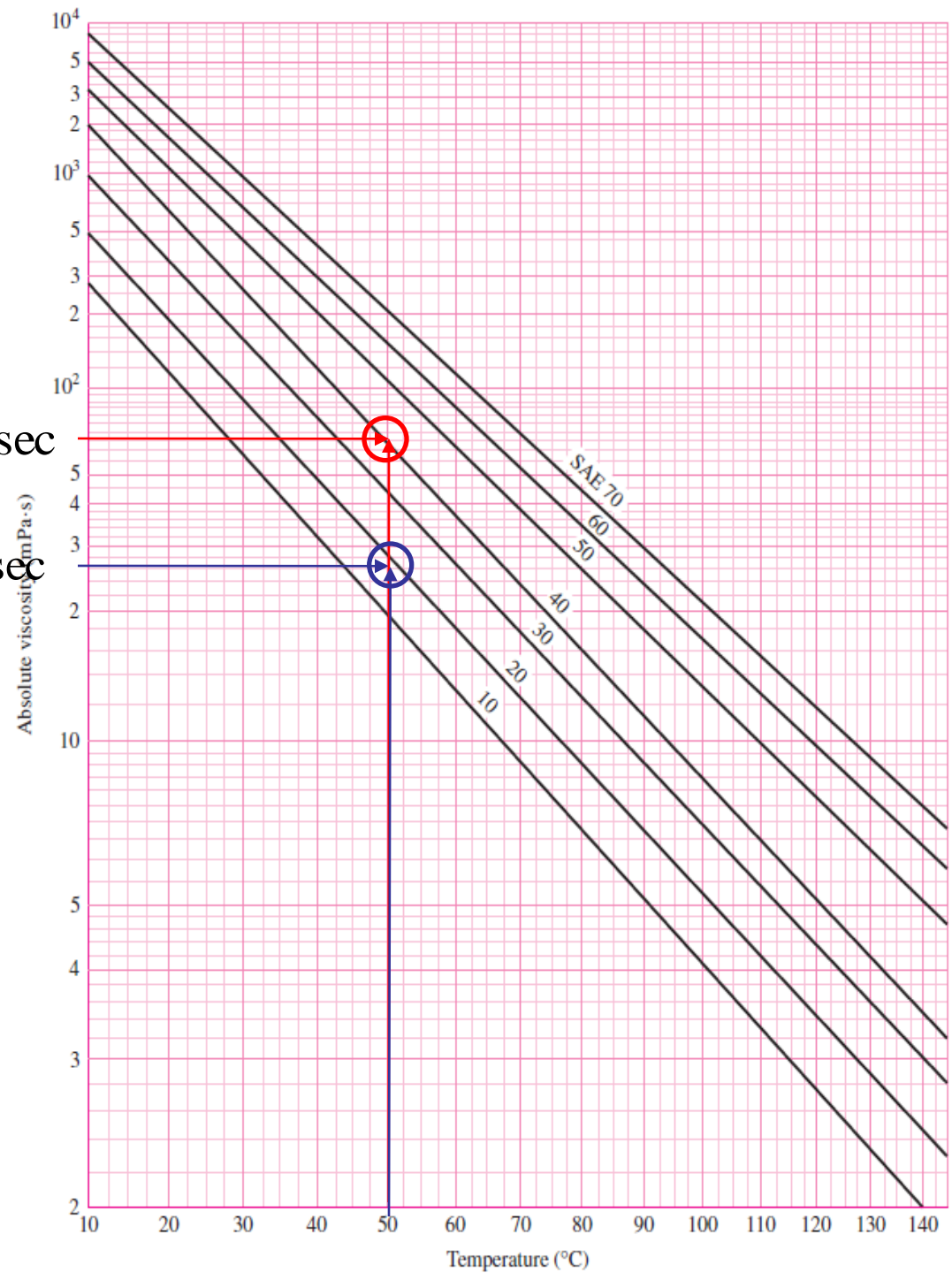
SAE 40 is the most suitable one for max. W

$$\mu = 67.6 \text{ mPa}\cdot\text{sec}$$

$$\mu = 25.75 \text{ mPa}\cdot\text{sec}$$

and SAE 20 is suitable for f_{\min}

$$T_{ave} = 50 \text{ }^\circ\text{C} \text{ for both cases}$$



6) Now because S and l/d are known most other parameters can be determined from Boyd chart ($S=0.21$ and $l/d=1$):

$$\left(\frac{r}{c}\right)f = 4.8 \quad (\text{p540})(\text{p444}) \rightarrow \rightarrow f = 4.8 \left(\frac{c}{r}\right) = 4.8 \frac{0.05}{40} = 0.006$$

$$\frac{Q}{rcNl} = 4.1 \quad (\text{p541})(\text{p445}) \rightarrow \rightarrow Q = 4.1rcNl = 3280 \quad \text{mm}^3/\text{sec}$$

$$\frac{Q_s}{Q} = 0.55 \quad (\text{p542})(\text{p446}) \rightarrow \rightarrow Q_s = 0.55 \times 3280 = 1804 \quad \text{mm}^3/\text{sec}$$

$$\frac{P}{P_{\max}} = 0.46 \quad (\text{p543})(\text{p446}) \rightarrow \rightarrow P_{\max} = \frac{P}{0.46} = \frac{1.031 \text{MPa}}{0.46} = 2.241 \quad \text{MPa}$$

$$\frac{h_0}{c} = 0.53 \quad (\text{p543})(\text{p446}) \rightarrow \rightarrow h_0 = 0.53 \times c = 0.0256 \text{mm} = 25.6 \mu\text{m}$$

7)

$$\Delta T_{o_c} = \frac{8.30P}{\left[1 - \frac{1}{2} \times \frac{Q_s}{Q}\right]} \times \frac{\frac{r}{c} f}{\frac{Q}{rcNl}} = \frac{8.3 \times 1.031 \text{ MPa}}{1 - \frac{1}{2} \times 0.05} \times \frac{4.8}{4.1} = 13.8 \text{ } ^\circ\text{C}$$

$$\Delta T_{o_c} = T_{\text{var}} \frac{P}{\gamma C_H} = ?? \text{ } ^\circ\text{C} \quad T_v = ?$$

Fig.12.12 ($S = 0.21$), $\frac{l}{d} = 1 \rightarrow \rightarrow T_v = 20$

$$\Delta T_{o_c} = 20 \times \frac{1.031 \times 10^6}{861 \times 1760} = 13.7 \text{ } ^\circ\text{C}$$

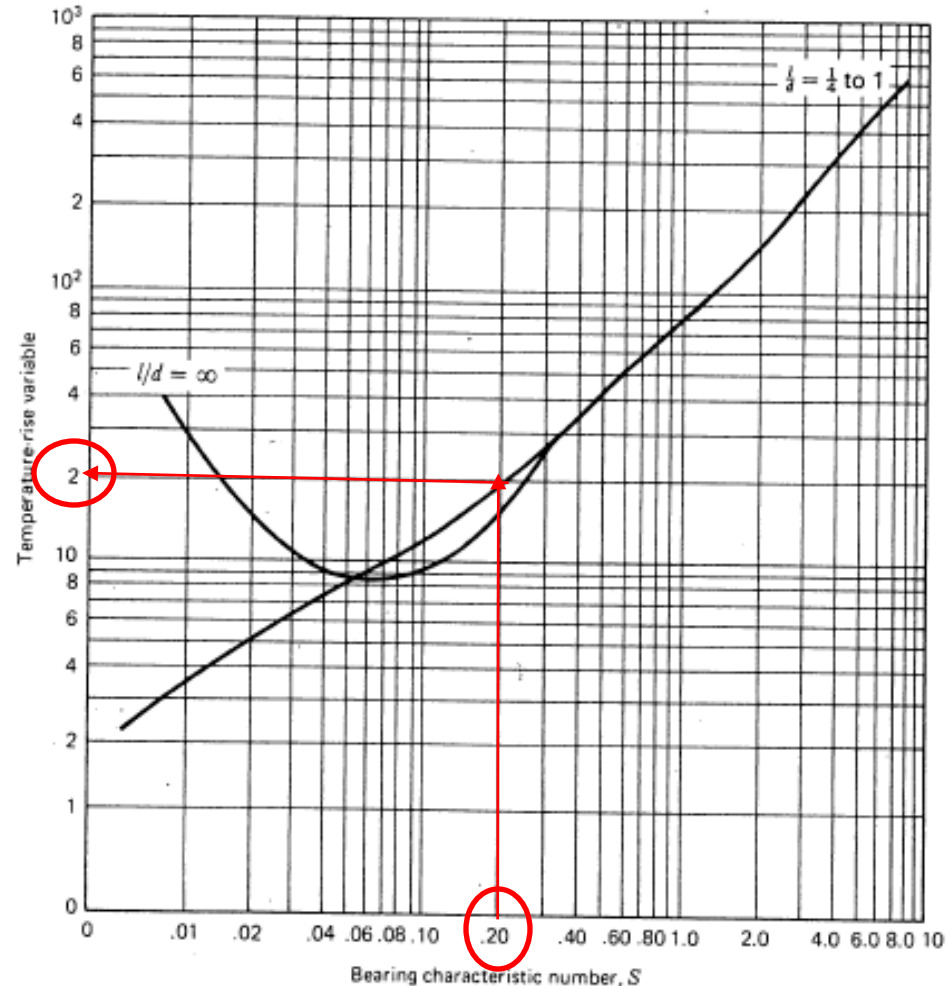


FIGURE 12-12 Chart for temperature-rise variable $T(\text{var}) = \gamma C_H \Delta T/P$. In plotting this chart it was found that the curves for $l/d = \frac{1}{4}, \frac{1}{2},$ and 1 were so close together that they could not be distinguished from a single curve.

8) The torque required to overcome the friction is

$$T_f = f \times W \times r = 0.006 \times 6600 \times 0.04 = 1.584 \text{ Nm} \quad \text{For max W cond } S=0.21 \text{ and } l/d=1$$

$$T_f = f \times W \times r = 0.003 \times 6600 \times 0.04 = 0.792 \text{ Nm} \quad \text{For min friction cond } S=0.08 \text{ and } l/d=1$$

The power loss is

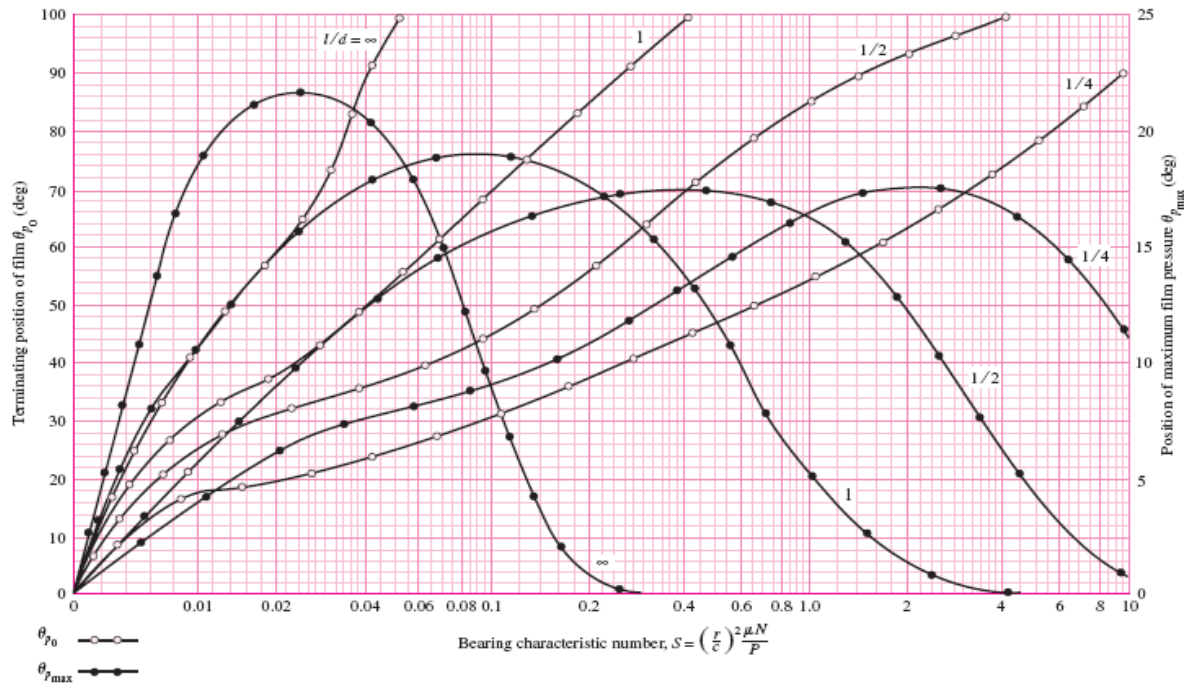
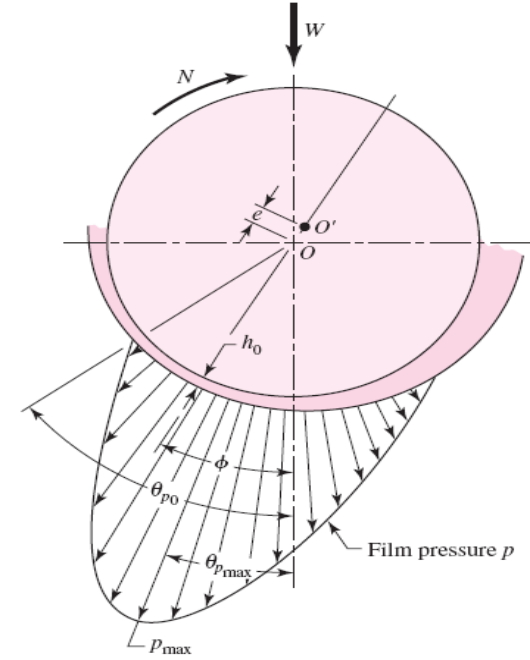
$$P_{loss} = T_f \times \omega_{\frac{rad}{sec}} = 1.585 \times 300 \frac{rev}{min} \times \frac{min}{60sec} \times \frac{2\pi rad}{rev} = 49.76 \text{ Nm/sec}$$

$$P_{loss} = 49.76 \text{ watt} \quad \text{For max W cond } S=0.21 \text{ and } l/d=1$$

$$P_{loss} = 24.88 \text{ watt} \quad \text{For min friction cond } S=0.08 \text{ and } l/d=1$$

if required $(\theta_{P_0} \ \& \ \theta_{P_{max}})$ for $S = 0.21, \frac{l}{d} = 1$
 from Fig. 12.21 p554

$$\theta_{P_0} = 85^\circ \ \& \ \theta_{P_{max}} = 21.25^\circ$$



OPTIMIZATION OF J.B's

In designing a journal bearing for thick-film lubrication, the engineer must :

- select the grade of oil to be used and
- determine suitable values for P , N , r , c , and l .

A poor selection of these parameters or inadequate control of them during manufacture or in use may result in a film that is too thin, so that the oil flow is insufficient, causing the bearing to overheat and, eventually, fail.

Furthermore, the radial clearance c is difficult to hold accurate during manufacture, and it may increase because of wear.

What is the effect of an entire range of radial clearances, expected in manufacture, and what will happen to the bearing performance if c increases because of wear?

Most of these questions can be answered and the design optimized by plotting curves of the performance as functions of the quantities over which the designer has control.

Figure shows the results obtained when the performance of a particular bearing is calculated for a whole range of radial clearances and is plotted with clearance as the independent variable.

The graph shows that if the clearance is too tight, the outlet temperature T_2 will be too high and the minimum film thickness (h_o) too low.

High temperatures may cause the bearing to fail by fatigue. If the oil film is too thin, dirt particles may be unable to pass without scoring or may embed themselves in the bearing.

In either event, there will be excessive wear and friction, resulting in high temperatures and possible seizing.

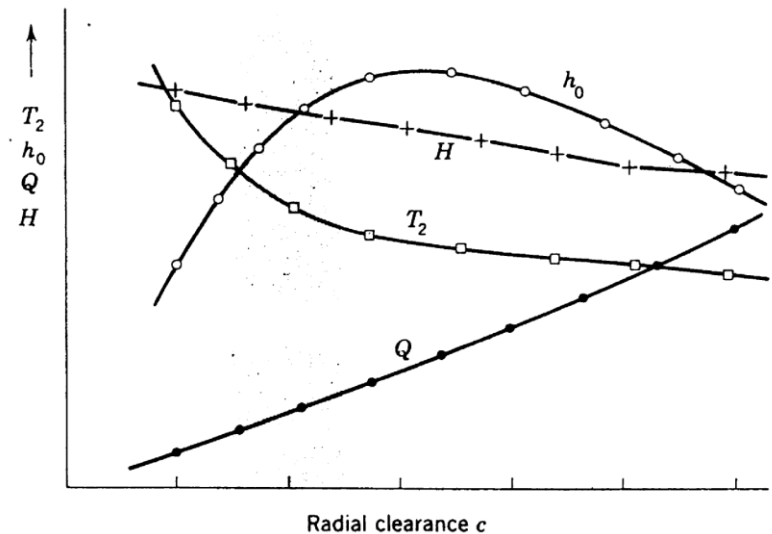


FIGURE 12-21 A plot of some performance characteristics. The bearing outlet temperature is T_2 . New bearings should be designed for the shaded zone because wear will move the operating point to the right.

A tight clearance results in a high temperature. It would seem that a large clearance will permit the dirt particles to pass through and also will permit a large flow of oil. This lowers the temperature and increases the life of the bearing. However, if the clearance becomes too large, the bearing becomes noisy and the minimum film thickness begins to decrease again.

In between these two limitations there exists a rather large range of clearances that will result in satisfactory bearing performance.

When both the production tolerance and the future wear on the bearing are considered, it is seen, from Fig. 12-25, that the best compromise is a clearance range slightly to the left of the top of the minimum-film-thickness curve.

In this way, future wear will move the operating point to the right and increase the film thickness and decrease the operating temperature

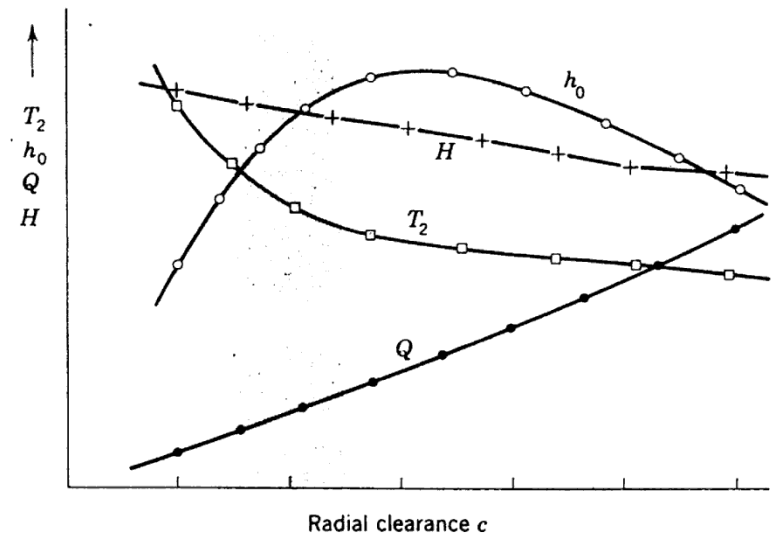


FIGURE 12-21 A plot of some performance characteristics. The bearing outlet temperature is T_2 . New bearings should be designed for the shaded zone because wear will move the operating point to the right.

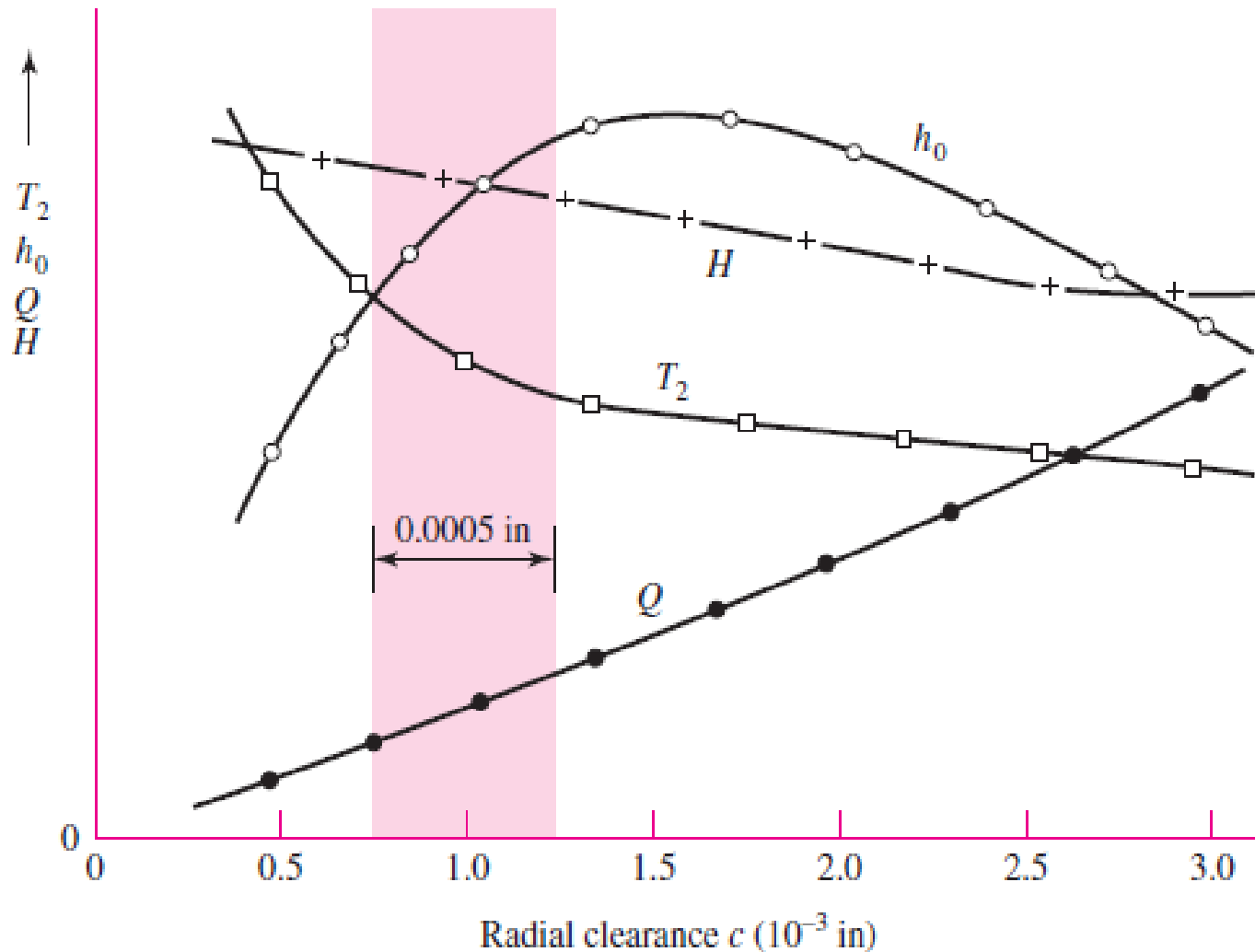


Fig 12.25 A plot of some performance characteristics of the bearing of Exs. 12–1 to 12–4 for radial clearances of 0.0005 to 0.003 in. The bearing outlet temperature is designated T_2 . New bearings should be designed for the shaded zone, because wear will move the operating point to the right.

PRESSURE - FED BEARINGS (HYDRO-STATIC JOURNAL BEARING)

The load-carrying capacity of self-contained natural-circulating (hydro-dynamic) journal bearings is quite restricted.

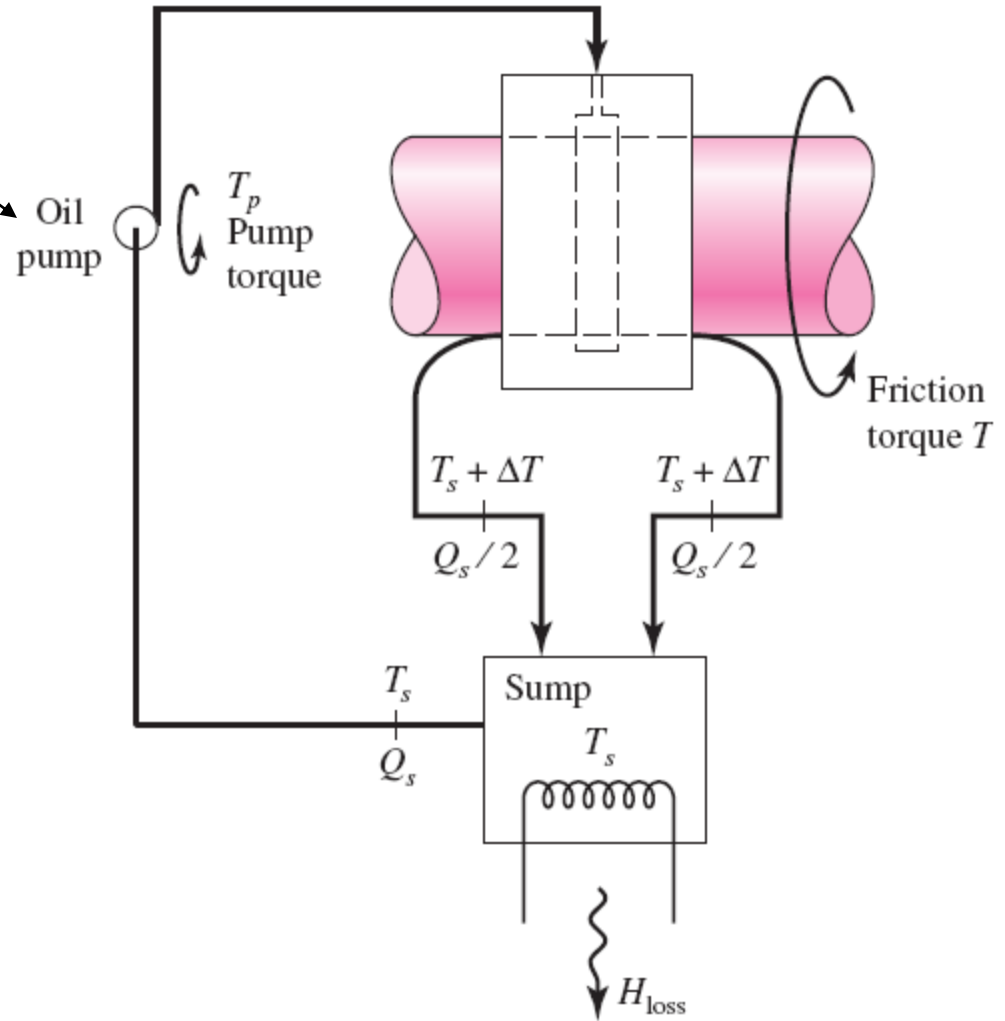
The factor limiting better performance is usually the heat-dissipation capability of the bearing.

A first thought of a way to increase heat dissipation is to cool the sump with an external fluid such as water. The high-temperature problem is in the film where the heat is generated but cooling is not possible in the film until later. This does not protect against exceeding the maximum allowable temperature of the lubricant.

A second alternative is to reduce the *temperature rise* in the film by dramatically increasing the rate of lubricant flow.

To increase lubricant flow, an external pump must be used with lubricant supplied at pressures higher than atmospheric pressure.

Because the lubricant is supplied to the bearing under pressure, such bearings are called **pressure-fed bearings**.



To force a greater flow through the bearing and thus obtain an increased cooling effect, a common practice is to use a circumferential groove at the center of the bearing, with an oil-supply hole located opposite the load-bearing zone.

Such a bearing is shown in Fig. 12–27. The effect of the groove is to create two half-bearings, each having a smaller l/d ratio than the original.

The groove divides the pressure-distribution curve into two lobes and reduces the minimum film thickness, but it has wide acceptance among lubrication engineers because such bearings carry more load without overheating.

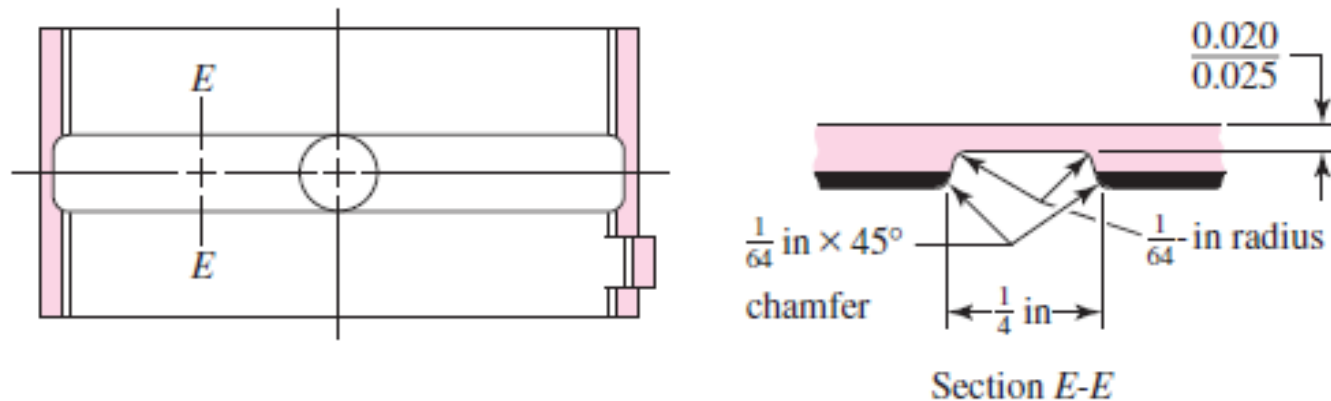
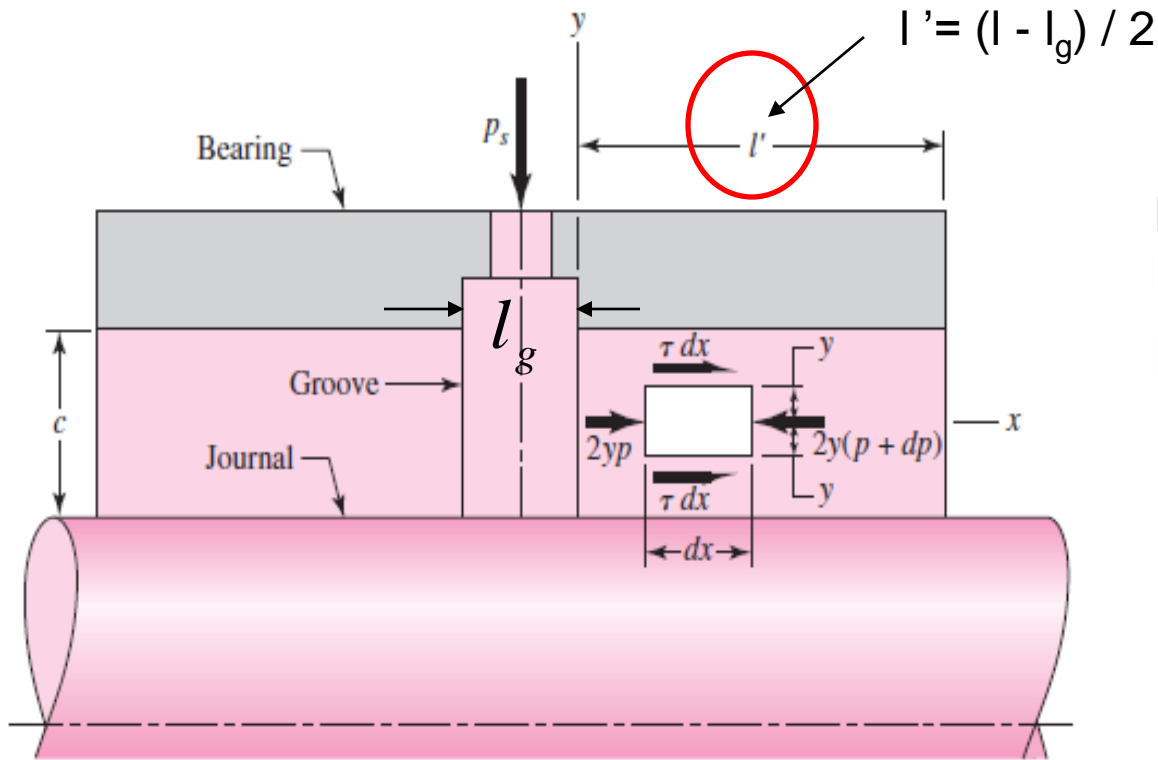


Fig. 12.27 Centrally located full annular groove.



Here we assume that the bearing is two fold each having properties:

l'/d (instead of l/d) and

$P = (W/2)/(l'd)$

$$P = \frac{W/2}{l' * d}$$

Fig. 12.28 Flow of lubricant from a pressure-fed bearing having a central annular groove.

These pressure-fed (hydro-static) bearings do not rely on wedging action of the lubricant by the rotation of journal only but lubricant is forced into the bearing clearance under a pressure p_s

This is the method used in application where the normal lubricant flow Q is not sufficient to carry away the heat generated by the hydrodynamic action within the bearing clearance for the load carried is high to be hold up.

Therefore “a special oil flowrate formula Q ” will be developed for pressure-fed (hydro-static) bearings. The Q_s/Q and $Q/rcNI$ figures will NOT be used.

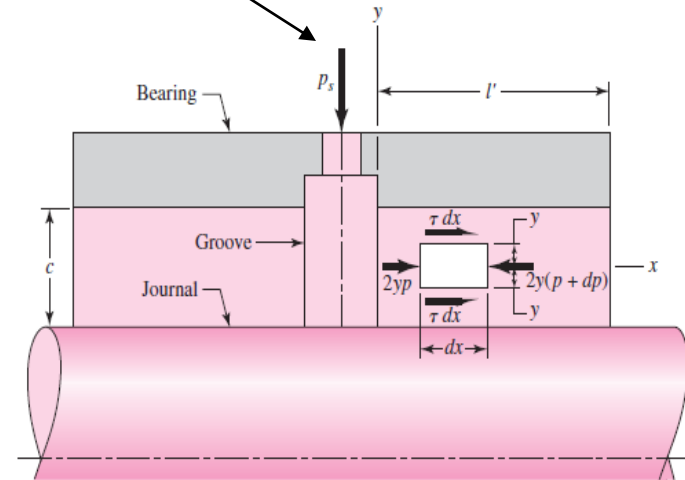
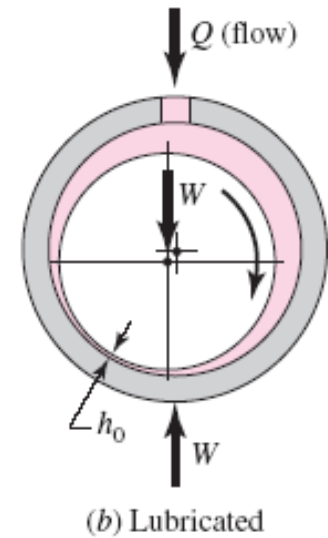


Figure 12–29 shows a graph of this relation fitted into the clearance space c so that you can see how the velocity of the lubricant varies from the journal surface to the bearing surface.

The distribution is parabolic, as shown, with the maximum velocity occurring at the center, where $y = 0$. The magnitude is, from Eq. (12–21),

$$u_{\max} = \frac{p_s c^2}{8\mu l'} \quad (i)$$

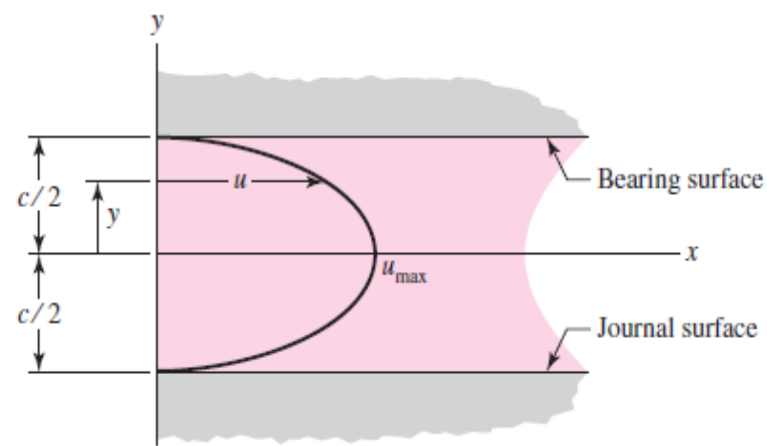


Fig.12.29 Parabolic distribution of the lubricant velocity.

To consider eccentricity, as shown in Fig. 12–30, the film thickness is $h = c - e \cos \theta$. Substituting h for c in Eq. (i), with the average ordinate of a parabola being two-thirds the maximum, the average velocity at any angular position θ is

$$u_{ave} = \frac{2}{3} \frac{p_s h^2}{8\mu l'} = \frac{p_s}{12\mu l'} (c - e \cos \theta)^2 \quad (j)$$

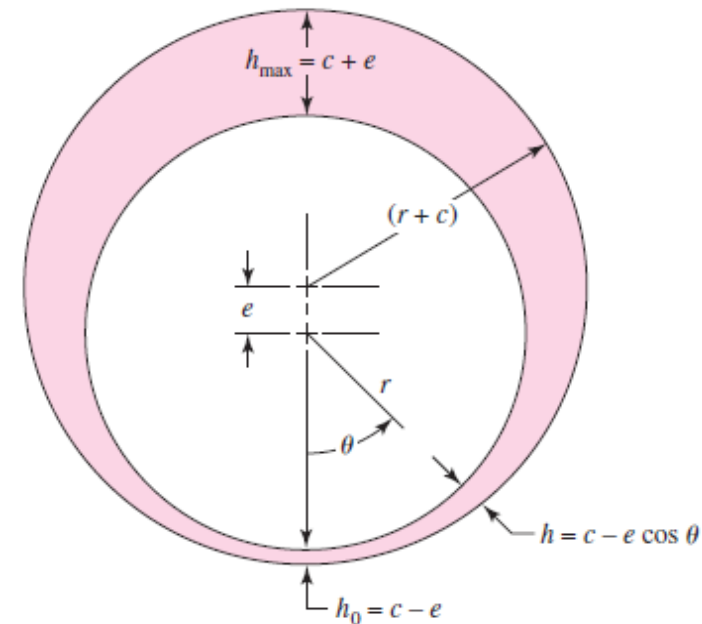


Fig. 12.30

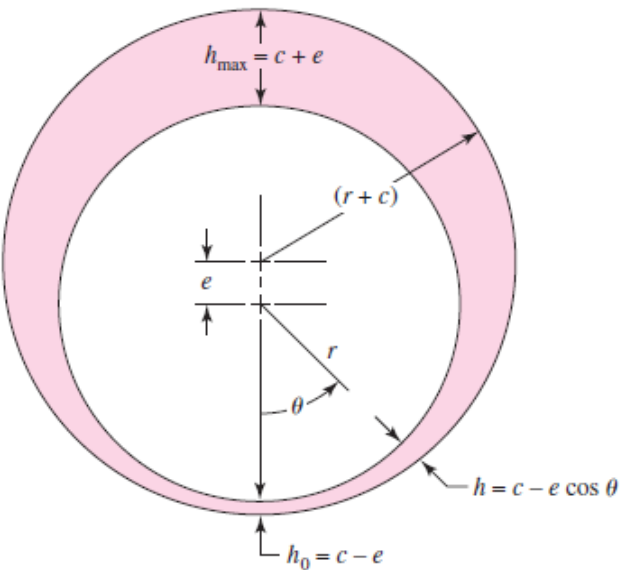


Fig. 12.30

$$h_o = c(1 - \varepsilon)$$

$$\varepsilon = \frac{e}{c}$$

We can compute the amount of lubricant that flows out both ends;

$$dQ_s = u_{ave} \times dA \quad dA = h \times r d\theta$$

Total side flow is twice that value and dA is the elemental area;

$$dQ_s = 2 \times u_{ave} \times h r d\theta$$

$$u_{ave} = \frac{p_s}{12\mu l'} (c - e \cos \theta)^2$$

$$dQ_s = \frac{p_s r}{6\mu l'} (c - e \cos \theta)^3 d\theta$$

Integrating around the bearing gives the total side flow as

$$Q_s = \int dQ_s = \frac{P_s r}{6\mu l'} \int_0^{2\pi} (c - e \cos \theta)^3 d\theta = \frac{P_s r}{6\mu l'} (2\pi c^3 - 3\pi c^3)$$

Rearranging, with $\varepsilon = e/c$, gives

$$Q_s = \frac{\pi p_s r c^3}{3\mu l'} (1 + 1.5\varepsilon^2)$$

Flow rate eqn for pressure-fed bearings

The charts for
flow variable ($Q/rcNl$) and
flow ratio (Q_s/Q) (Figs. 12–19 and 12–20)
DO NOT apply to pressure-fed bearings.

In analyzing the performance of pressure-fed bearings, **the bearing length should be taken as l'** .

The characteristic pressure in each of the two bearings that constitute the pressure-fed bearing assembly P is given by

$$P = \frac{W / 2}{2rl'} = \frac{W}{4rl'}$$

Also, the maximum film pressure P_{\max} given by Fig. 12–21 must be increased by the oil supply pressure p_s to obtain the total film pressure.

$$P_{\max} = P_{\max} + P_s$$

Since the oil flow has been increased by forced feed, Eq. (12–14) will not give a correct temperature rise (will give too high temp rise) because the side flow carries away all the heat generated. A new temp. rise eqn (ΔT) is derived for pressure fed bearings.

To calculate heat gain- temperature rise (ΔT)- of the fluid passing through the bearing the following steps are followed:

$$1) \quad \frac{l'}{d} = \frac{(l - l_g) / 2}{d} \qquad 2) \quad P = \frac{W / 2}{2rl'} = \frac{W}{4rl'}$$

The Sommerfeld number may be expressed as

$$3) \quad S = \left(\frac{r}{c}\right)^2 \frac{\mu N}{P} = \left(\frac{r}{c}\right)^2 \frac{\mu N}{\frac{W}{4rl'}} = \left(\frac{r}{c}\right)^2 \frac{4rl' \mu N}{W}$$

4) The corresponding temperature rise (ΔT) equation in SI units uses the bearing load W in kN, lubricant supply pressure p_s in kPa, and the journal radius r in mm:

$$\Delta T_{oc} = \frac{978 \times 10^6}{1 + 1.5 \varepsilon^2} \times \frac{\left(\frac{r}{c} f\right) S W^2}{p_s r^4}$$

Where ΔT in °C (temperature increase)
 W = bearing load in kN
 p_s = supply pressure in kPa
 r = journal radius in mm

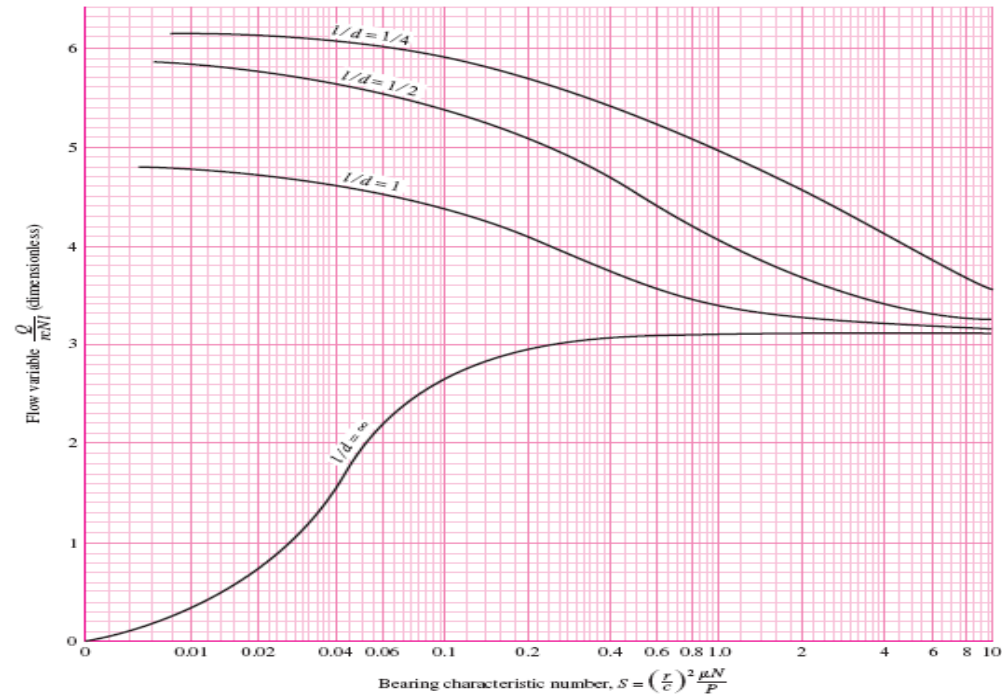
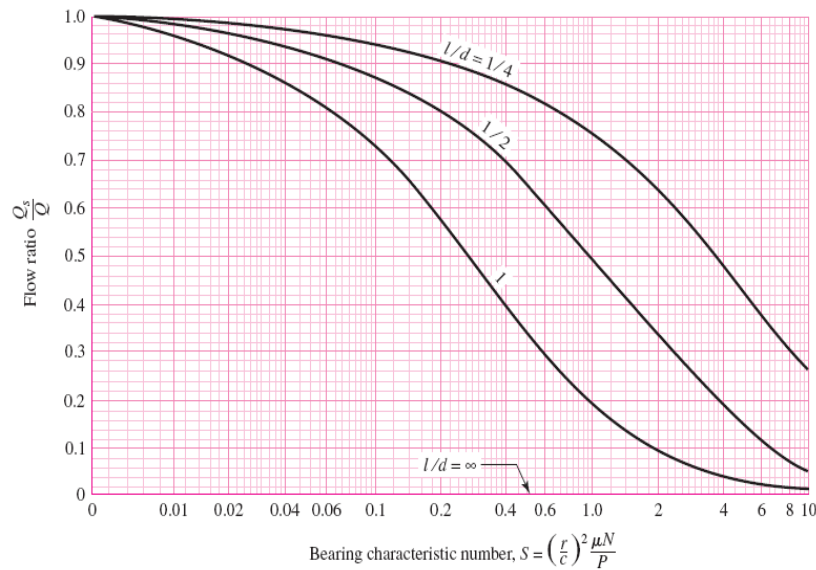
OR YOU CAN USE

$$\Delta T_{oc} = \frac{1.5 \left(\frac{r}{c} f\right)}{\gamma C_H (1 + 1.5 \varepsilon^2)} \times \frac{S W^2}{p_s r^4}$$

Where $\gamma = 861 \text{ kg/m}^3$
 $C_H = 1760 \text{ J/kg } ^\circ\text{C}$
 W = bearing load in N
 p_s = supply pressure in Pa
 r = journal radius in m

5) **DO NOT** use figures 12.18 (17) of flow rate variable

and 12.19 (18) flow rate



Instead, use the equation

$$Q_s = \frac{\pi p_s r c^3}{3 \mu l'} (1 + 1.5 \varepsilon^2)$$

6) Use figures 12.20 (40) but to find maximum pressure add two values P_{\max} & p_s .

$$P_{\max \text{ act}} = P_{\max} + p_s$$

Example 3: (12-20) (prob 12.16)

An 8- cylinder diesel engine has a front main bearing 90 mm in diameter and 51 mm long. The bearing has a central annular oil groove 6 mm wide.

It is pressure lubricated with SAE 30 oil at an inlet temperature of 82 °C and at a supply pressure of 345 kPa.

Corresponding to a radial clearance of 0.064 mm, a speed of 2800 rpm and a radial load of 20500 N, find;

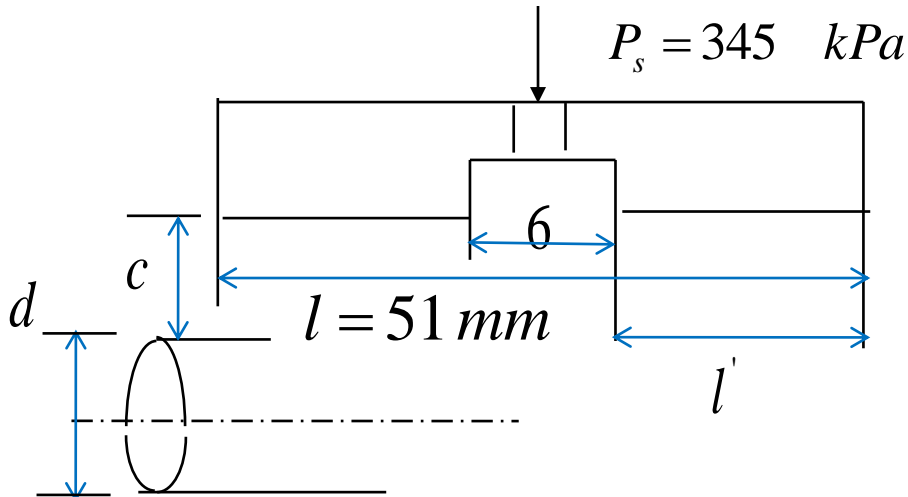
a) The temperature rise

b) Minimum oil film thickness

e) θ_{h_0} & $\theta_{P_{\max}}$

c) maximum oil film pressure

d) oil flow



$$l = 51 \text{ mm}$$

$$d = 90 \text{ mm} \rightarrow r = 45 \text{ mm}$$

$$l_g = 6 \text{ mm} \rightarrow l' = \frac{1}{2}(l - l_g) = 22.5 \text{ mm}$$

$$\frac{l'}{d} = \frac{22.5}{90} = \frac{1}{4}$$

$$T_i = 82 \text{ } ^\circ\text{C}$$

$T_o = ? \quad \mapsto \mu \text{ at } T_{ave}$ Since ΔT & μ are unknowns we need to use trail and error method

$$P_s = 345 \text{ kPa}$$

$$c = 0.064 \text{ mm}$$

$$r = 45 \text{ mm}$$

$$n = 2800 \text{ rpm} \rightarrow N = 46.7 \text{ rev/sec}$$

$$W = 20500 \text{ N}$$

$$P = \frac{W}{4rl} = \frac{20500}{4 \times 45 \times 22.5} = 5.06 \text{ MPa}$$

(see pp.558 Table 12.2, 6-12 MPa)

a)

$$\Delta T_{oc} = \frac{978 \times 10^6}{1 + 1.5\varepsilon^2} \times \frac{\left(\frac{r}{c} f\right) S W^2}{p_s r^4} \quad \text{where } \varepsilon \text{ \& } \frac{r}{c} f \text{ depends on } S \text{ \& } \frac{l}{d}$$

but $S = \left(\frac{r}{c}\right)^2 \frac{\mu N}{P}$ depends on μ

also μ depends on $T_i + \frac{\Delta T}{2}$

Start by assuming $\Delta T = 20 \text{ }^\circ\text{C}$

$$T_{ave} = T_i + \frac{\Delta T}{2} = 82 + 10 = 92 \text{ }^\circ\text{C} \rightarrow \mu = 8.5 \times 10^{-3} \text{ Pa-sec}$$

$$\text{Then } S = \left(\frac{45}{0.064}\right)^2 \frac{8.5 \times 10^{-3} \times 46.7}{5.06 \times 10^6} = 0.038$$

$$\text{For } S = 0.038 \quad \frac{h_0}{c} = 0.075 \quad \& \quad \varepsilon = 0.925 \quad (\text{Fig.12.14 or 12.16})$$

$$\frac{l'}{d} = \frac{1}{4} \quad \frac{r}{c} f = 2.1 \quad (\text{Fig.12.17 or 12.18})$$

$$\Delta T_{oc} = \frac{978 \times 10^6}{1 + 1.5 \times (0.925)^2} \times \frac{2.1 \times 0.038 \times (20.5)^2}{345 \times (45)^4} = 10.15 \text{ } ^\circ\text{C} < 20 \text{ } ^\circ\text{C}$$

Re-try $\Delta T = 10^\circ\text{C}$

$$T_{ave} = T_i + \frac{\Delta T}{2} = 82 + 5 = 87 \text{ } ^\circ\text{C} \rightarrow \mu = 10 \times 10^{-3} \text{ Pa-sec}$$

$$\text{Then } S = \left(\frac{45}{0.064} \right)^2 \frac{10 \times 10^{-3} \times 46.7}{5.06 \times 10^6} = 0.045$$

For $S = 0.045$

$$\frac{l'}{d} = \frac{1}{4}$$

$$\frac{h_0}{c} = 0.08 \quad \& \quad \varepsilon = 0.92 \quad (\text{Fig.12.16})$$

$$\frac{r}{c} f = 2.3 \quad (\text{Fig.12.18})$$

$$\Delta T_{oc} = \frac{978 \times 10^6}{1 + 1.5 \times (0.92)^2} \times \frac{2.3 \times 0.045 \times (20.5)^2}{345 \times (45)^4} = 13.2(12.6) \text{ } ^\circ\text{C} > 10 \text{ } ^\circ\text{C}$$

Re-try $\Delta T = 11^\circ\text{C}$;

$$T_{ave} = T_i + \frac{\Delta T}{2} = 82 + 5.5 = 87.5 \text{ } ^\circ\text{C} \rightarrow \mu = 9.5 \times 10^{-3} \text{ Pa-sec}$$

$$\text{Then } S = \left(\frac{45}{0.064} \right)^2 \frac{9.5 \times 10^{-3} \times 46.7}{5.06 \times 10^6} = 0.042$$

$$\text{For } S = 0.042 \quad \frac{h_0}{c} = 0.075 \quad \& \quad \varepsilon = 0.925 \quad (\text{Fig.12.16})$$

$$\frac{l'}{d} = \frac{1}{4}$$

$$\frac{r}{c} f = 2.2 \quad (\text{Fig.12.18})$$

$$\Delta T_{oc} = \frac{978 \times 10^6}{1 + 1.5 \times (0.925)^2} \times \frac{2.2 \times 0.042 \times (20.5)^2}{345 \times (45)^4} = 11.75(11.25) \text{ } ^\circ\text{C} \cong 11 \text{ } ^\circ\text{C}$$

$$\Delta T_{oc} = 11.25 \text{ } ^\circ\text{C} \cong 11 \text{ } ^\circ\text{C} \quad \text{OK...}$$

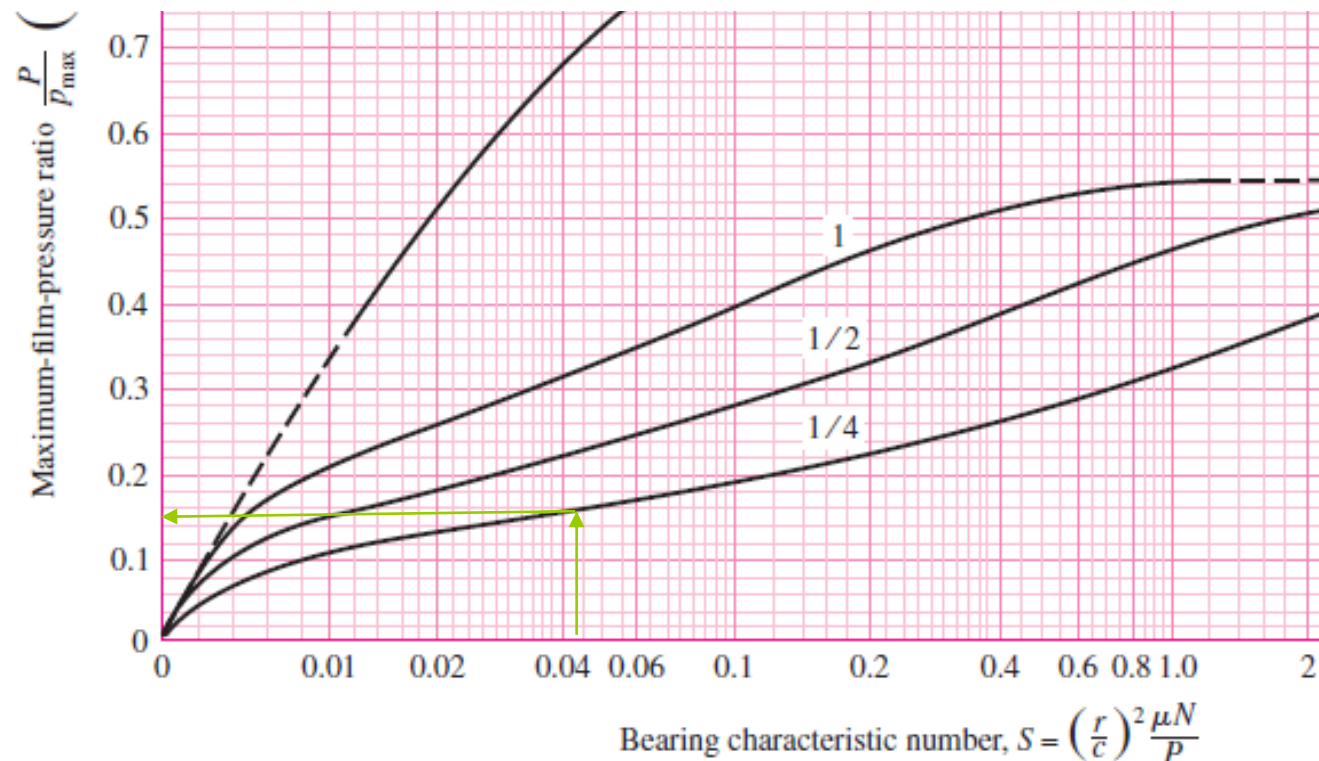
$$b) h_0 = 0.075 \times c = 0.075 \times 0.64$$

$$h_0 = 4.8 \times 10^{-3} \text{ mm} = 4.8 \text{ micron}$$

$$c) P_{\max} = ? \quad P_{\max} + P_s \quad \text{from Fig. 12.21 for } S = 0.042 \rightarrow \frac{P}{P_{\max}} = 0.15$$

$$\text{So, } P_{\max} = \frac{P}{0.15} = \frac{5.06}{0.15} = 33.73 \text{ MPa}$$

$$33.73 \times 10^6 + 345 \times 10^3 = 34078 \text{ kPa} = 34.078 \text{ MPa}$$



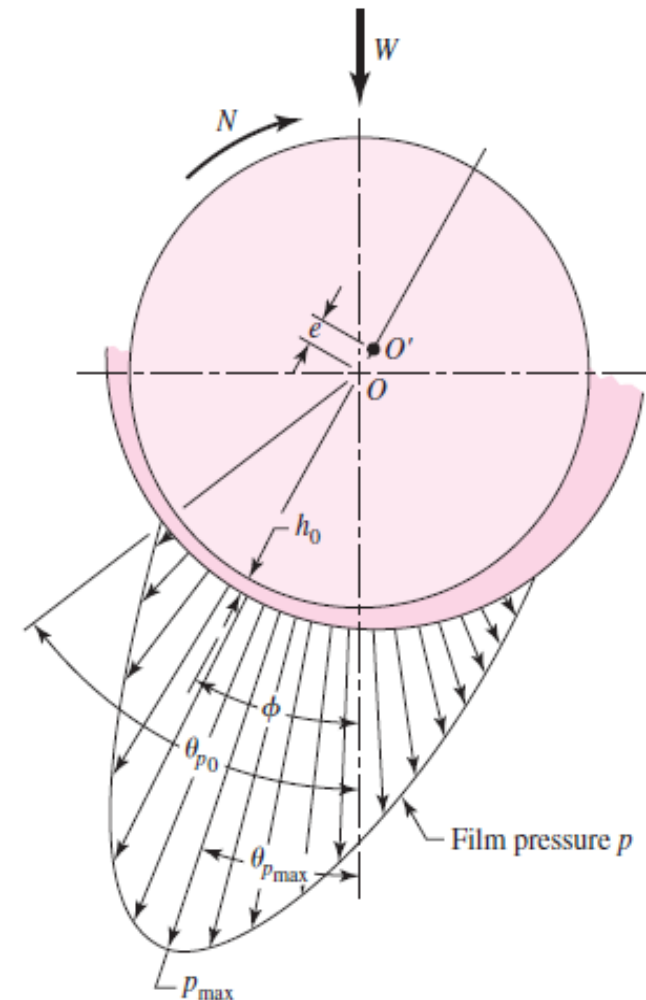
d) $Q_s = ?$

$$Q_s = \frac{\pi P_s r c^3}{3 \mu l'} (1 + 1.5 \varepsilon^2) = \frac{\pi \times 345 \times 10^3 \times 45 \times (0.064)^3}{3 \times 9.5 \times 10^{-3} \times 22.5} (1 + 1.5 \times (0.925)^2)$$

$$Q_s = 45528 \text{ mm}^3/\text{sec}$$

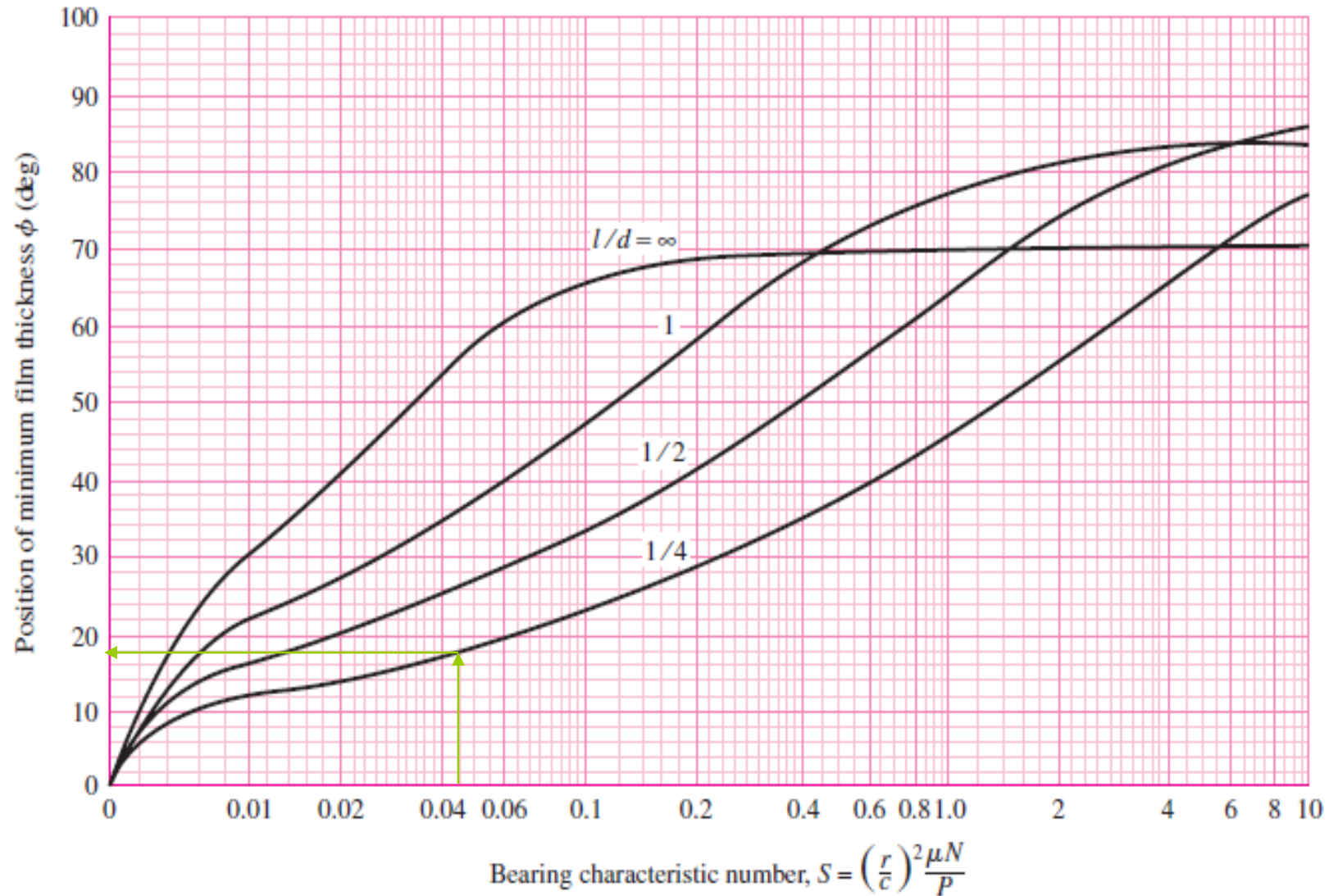
e)

For θ_{h_0} & $\theta_{P_{\max}}$ use related figures

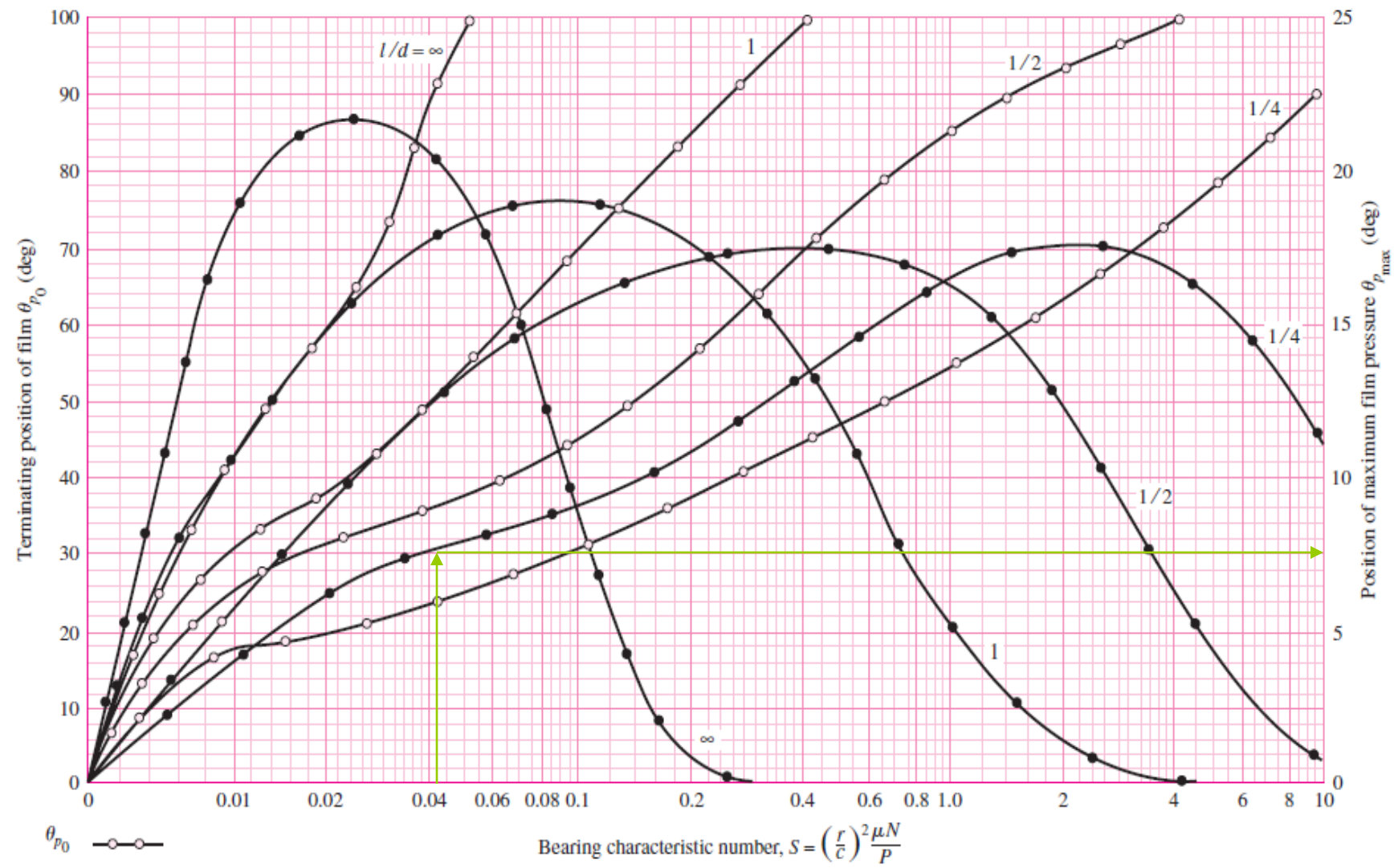


e)

For θ_{h0} & $\theta_{P_{\max}}$ use the Fig. 12.21



23.04.:



Design Suggestions

1. Start design (also analysis) by listing the given parameters
2. List the required parameters
3. Write down the relation between required parameters & the known parameters of $\Delta T = ?$ or $S = ?$
4. Use some recommended (suggested) values given in the tables & figures of P values & c values & PV_{max} values if not given in the problem or Assume them.
5. Start with an $l/d =$ unity if geometry of bearing is not fixed then increase this ratio if thin film lubrication is likely to occur decrease this ratio if thick film lubrication or high temperatures are likely to occur.

6. A long bearing (large l/d ratio) reduces the coefficient of friction & side flow and therefore is desirable where thin-film lubrication is present. On the other hand, a short bearing results in a greater flow of oil out of the end and thus keeping the bearing cooler. Where force – feed or positive lubrication ($P_s > 0$) is present. The l/d ratio should be relatively small.
7. If shaft deflection is likely to be severe, a short bearing should be used to prevent metal-to-metal contact at the ends of the bearing.
8. Always consider using of a partial bearing if high temperatures are a problem, because relieving the non-load bearing area of a bearing can very substantially reduce the heat generated.
9. Choose bearing material with satisfactory compressive and fatigue strength while having low melting point and low modulus of elasticity. (table 12-3) It should have resistance to wear and corrosion. It should have low friction coefficient (can be reduced by some design means)

Example 4:

A journal bearing has a diameter of 64 mm and length of 32 mm. The journal is to operate at a speed of 1800 rpm and carry a load of 3500 N. If SAE 20 oil at an inlet temperature of 44 °C is to be used. What should be the radial clearance for:

- a) Optimum load carrying capacity
- b) Minimum friction or power loss condition.

$$d = 64 \text{ mm} \rightarrow r = 32 \text{ mm}$$

$$l = 32 \text{ mm} \rightarrow l/d = 32/64 = 0,5$$

$$N = 1800 \text{ rpm} = 30 \text{ rps}$$

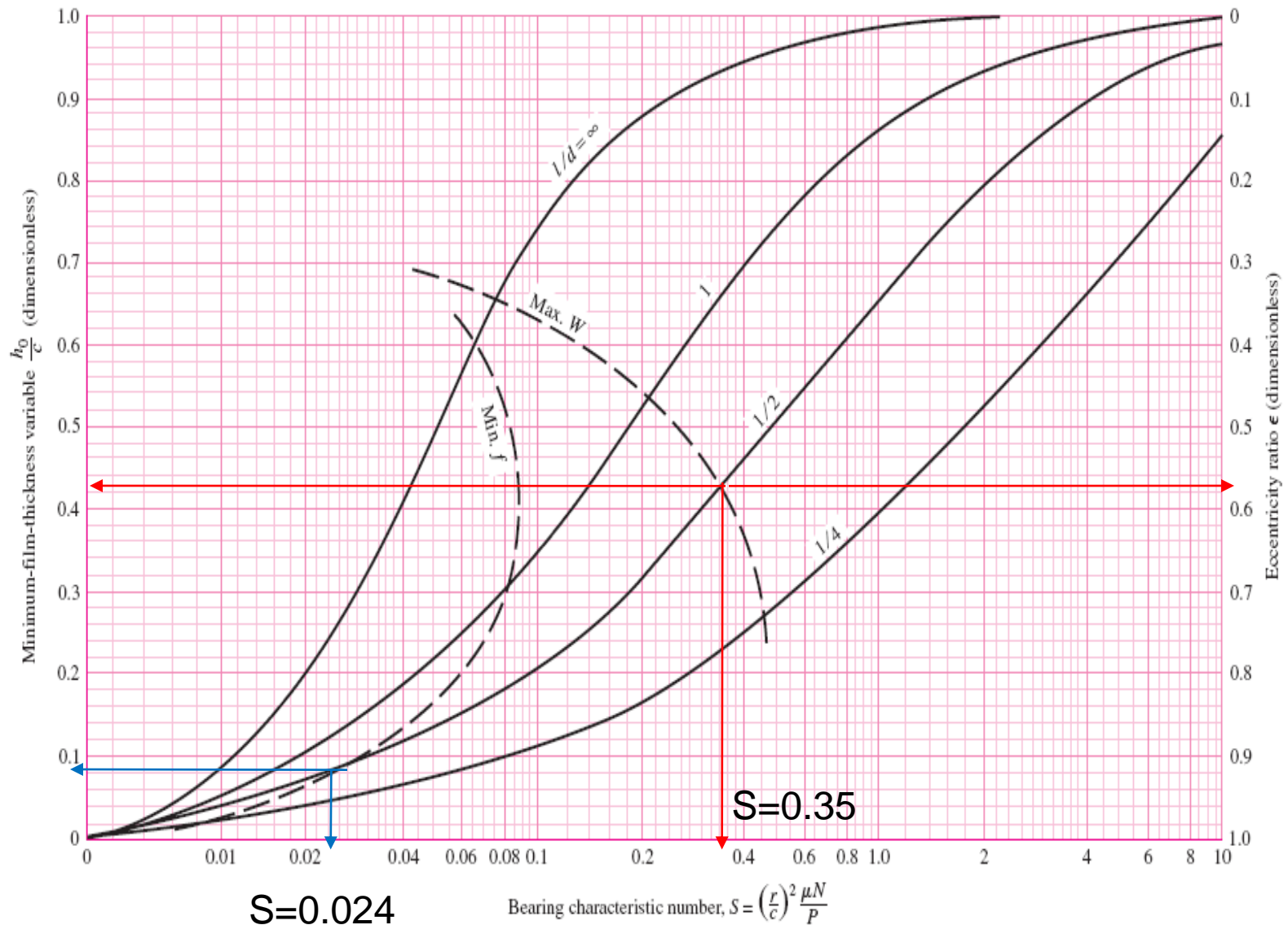
$$W = 3500 \text{ N}$$

$$T_i = 44^\circ\text{C}$$

SAE 20 oil

$$c = ?$$

a) For optimum load carrying capacity with $l/d = 1/2$



For $S = 0.35$

$$P = \frac{W}{l * d} = \frac{3500}{32 \times 64} = 1.709 \text{ MPa}$$

$$\frac{h_0}{c} = 0.425$$

$$\varepsilon = 0.575$$

For $S = 0.35$

$$\frac{l}{d} = \frac{1}{2}$$

$$\frac{r}{c} f = 9.0 \quad \& \quad T_{var} \cong 30$$

$$\frac{Q}{rcNl} = 4.8 \quad \& \quad \frac{Q_s}{Q} = 0.72$$

$$\Delta T_{oc} = \frac{8.30P}{\left[1 - \frac{1}{2} \times \frac{Q_s}{Q}\right]} \times \frac{\frac{r}{c} f}{\frac{Q}{rcNl}} = 41.55 \text{ } ^\circ C$$

$$\Delta T_{oc} = 30 * \frac{1.71 * E6}{\gamma * C_H} = 34C$$

$$T_{ave} = T_{in} + \frac{\Delta T}{2} = 44 + \frac{41.5}{2} = 64.75 \text{ } ^\circ C \rightarrow \mu = 15 \times 10^{-3} \text{ Pa} - \text{sec}$$

$$S = \left(\frac{r}{c}\right)^2 \frac{\mu N}{P} = 0.35 \quad c = \left[\frac{r^2}{S} \frac{\mu N}{P}\right]^{1/2} = 0.0277 \text{ mm} \cong 28 \text{ } \mu m$$

b) For minimum friction or power loss:

$$S = 0.024 \quad \& \quad \frac{h_0}{c} = 0.11$$

For $S = 0.024$

$$\frac{l}{d} = \frac{1}{2}$$

$$\frac{r}{c} f = 1.7 \quad \& \quad T_{\text{var}} \cong 7$$

$$\frac{Q}{rcNl} = 5.65 \quad \& \quad \frac{Q_s}{Q} = 0.94$$

$$\Delta T_{oC} = 7 * \frac{1.71 * E6}{\gamma * C_H} = 8C$$

$$\Delta T_{oC} = 8.05 \text{ } ^\circ\text{C} \quad (< \Delta T = 41.5 \text{ } ^\circ\text{C} \quad \text{based on max load})$$

$$T_{\text{ave}} = T_{\text{in}} + \frac{\Delta T}{2} = 44 + \frac{8.05}{2} = 48 \text{ } ^\circ\text{C} \quad \rightarrow \mu = 32 \times 10^{-3} \text{ Pa-sec}$$

$$c = \left[\frac{r^2 \mu N}{S P} \right]^{1/2} = \left[\frac{32^2 \cdot 32 \times 10^{-3} \times 30}{0.034 \cdot 1.709 \times 10^6} \right]^{1/2} = 0.13 \text{ mm} \cong 130 \mu\text{m}$$

$$130 \mu\text{m} > 28 \mu\text{m}$$

$$c_{fr} > c_{load}$$

Example 5:

A sleeve bearing is 100 mm diameter and has l/d ratio of 1/2. It has a frictional power loss of 100 watts when the load is 3000 N and the journal speed is 900 rpm for $c/r=0.002$.

a) Compute the minimum film thickness ($h_o=?$)

b) What is the viscosity of the oil and proper grade for an operating temperature of 71 °C ($T_{ave}=?$).

c) What is the temperature increase? $\Theta_{P_{max}}=?$ $P_{max}=?$

Solution:

Given:

$$\frac{l}{d} = \frac{1}{2} \quad d = 100 \text{ mm} \quad W = 3000 \text{ N} \quad P_{loss} = 100 \text{ watts}$$

$$N = 900 \text{ rpm} = 15 \text{ rps} \quad \frac{c}{r} = 0.002 \quad c = 0.002 \times 50 = 0.1 \text{ mm}$$

a) The frictional power loss is given by;

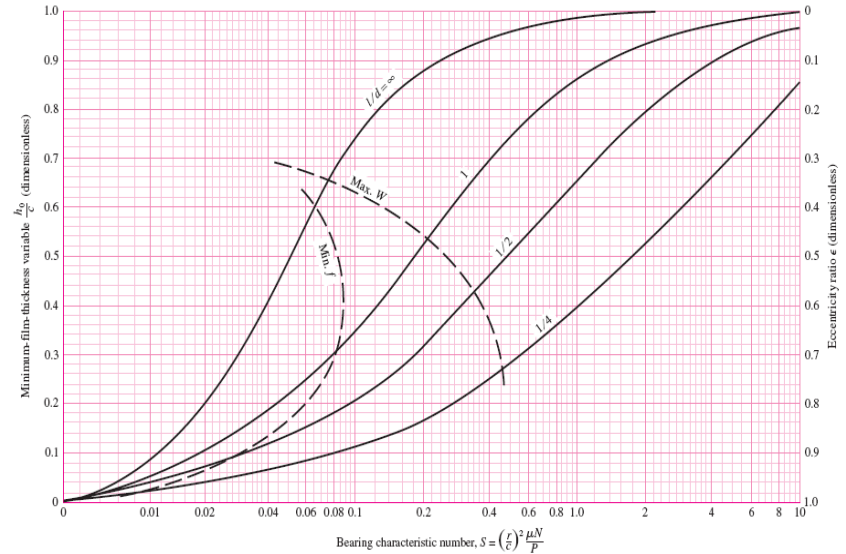
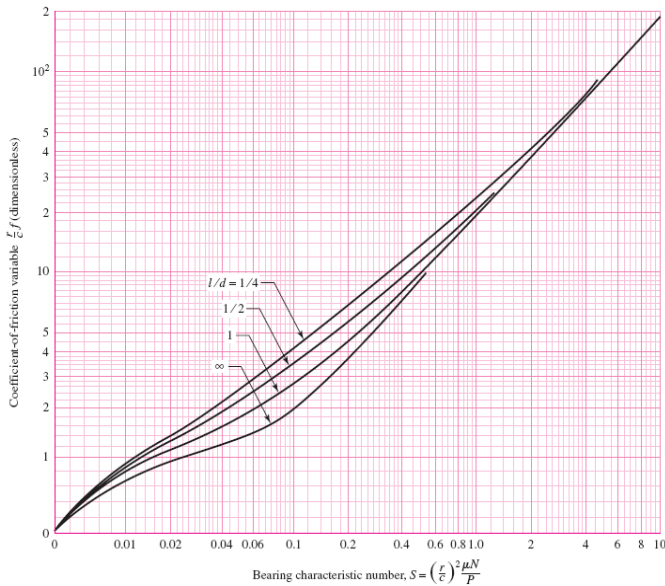
$$P_{loss} = T_{loss} \times \omega \frac{\text{rad}}{\text{sec}} = (f \times W \times r) \times (2\pi N)$$

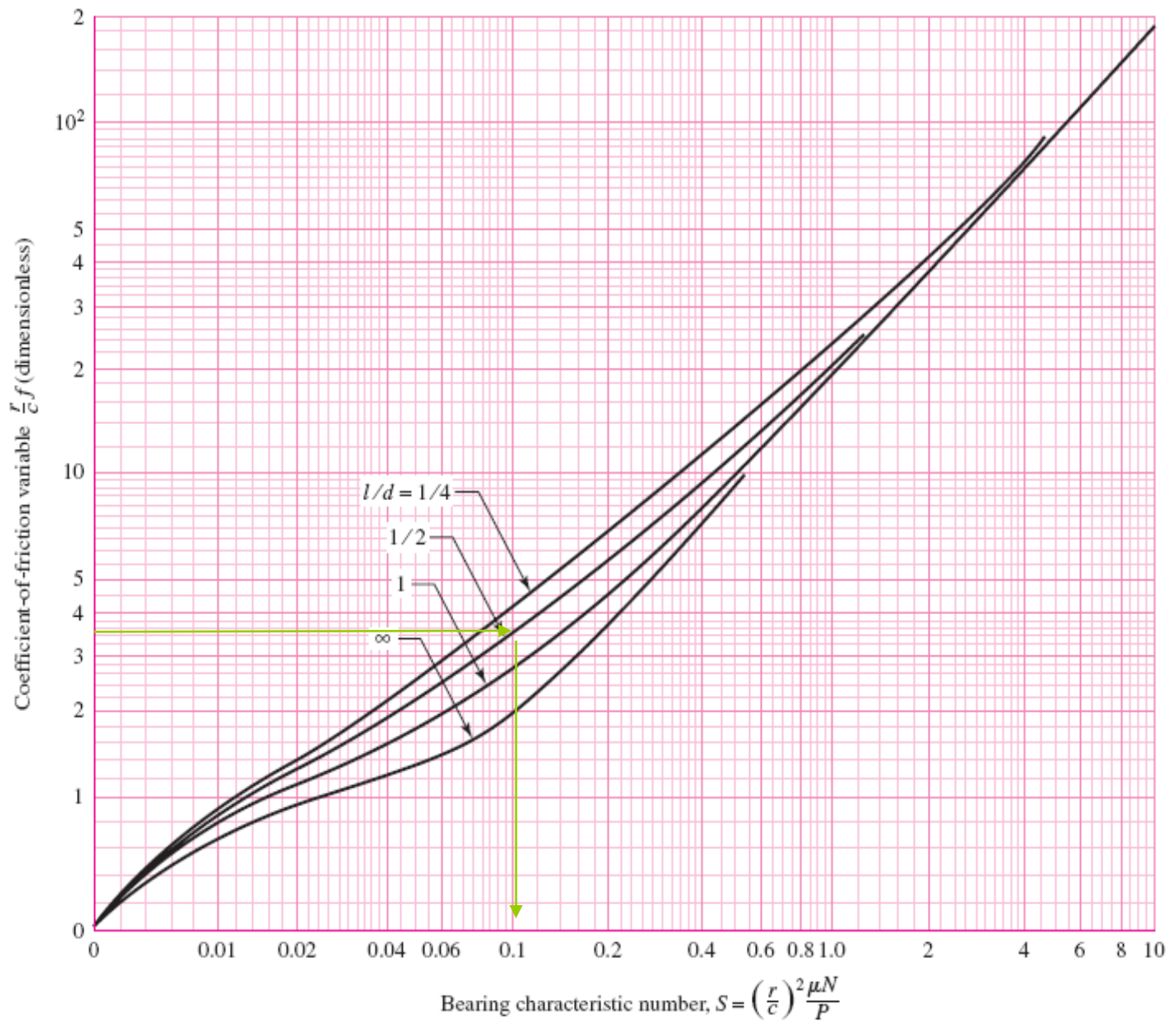
$$T_{loss} = F_{fric} \times r$$

$$F_{fric} = W \times f$$

where only f is unknown

$$f = \frac{P_{loss}}{W \times r \times 2\pi N} = \frac{100}{3000 \times 0.05 \times 2\pi \times 15} = 0.00707$$





from this figure S can be determined.

$$\frac{r}{c} = \frac{1}{0.002} = 500 \rightarrow \frac{r}{c} f = 3.535 \quad \& \quad \frac{l}{d} = \frac{1}{2}; \quad \underline{\underline{S = 0.1}}$$

$$\frac{h_0}{c} = 0.21 \rightarrow h_0 = 0.21 \times c = 0.021 \text{ mm} \quad \underline{\underline{h_0 = 21 \mu\text{m}}}$$

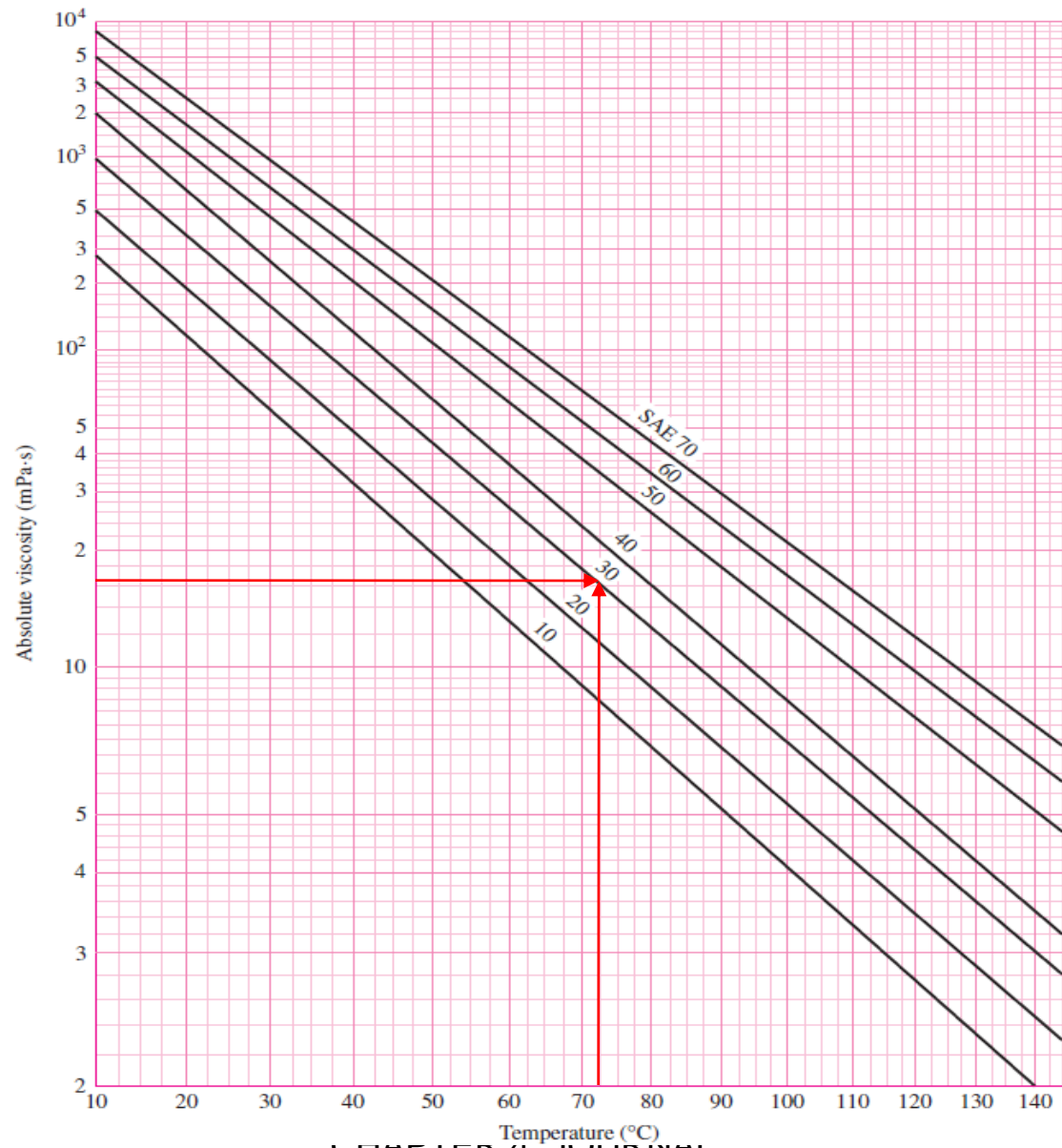
b)

$$S = \left(\frac{r}{c}\right)^2 \frac{\mu N}{P} \quad P = \frac{W}{ld} = \frac{3000}{50 \times 100} = 0.6 \text{ MPa}$$

$$\mu = \frac{SP}{N \left(\frac{r}{c}\right)^2} = \frac{0.1 \times 0.6 \times 10^6}{15(500)^2} = 0.016 \text{ Pa} - \text{sec} = \underline{\underline{16 \text{ mPa} - \text{sec}}}$$

For operating temperature of 71 oC ($T_{ave}=71$).
SAE 30 is the suitable one to be used.

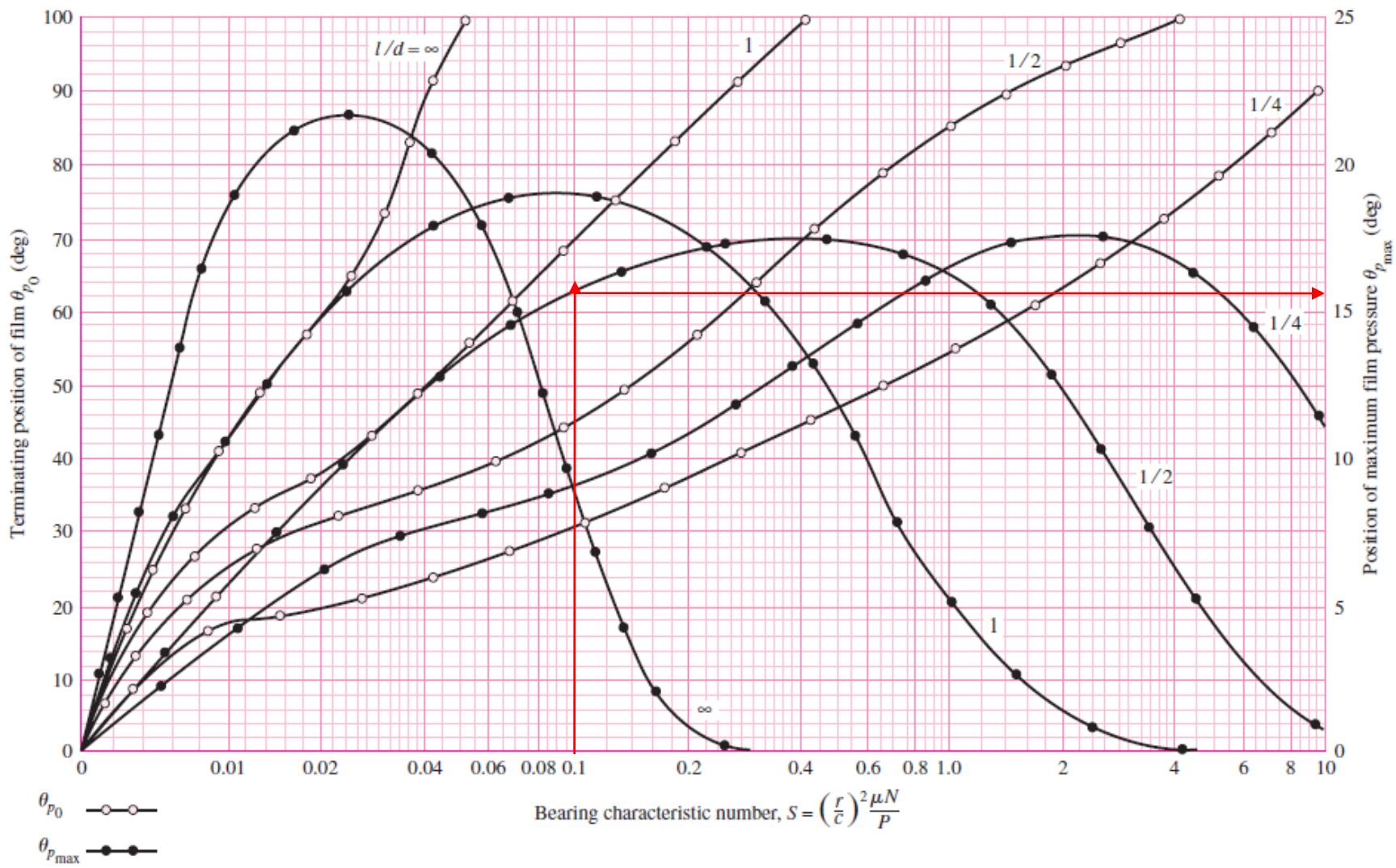
SAE 30 is the suitable oil to be used.

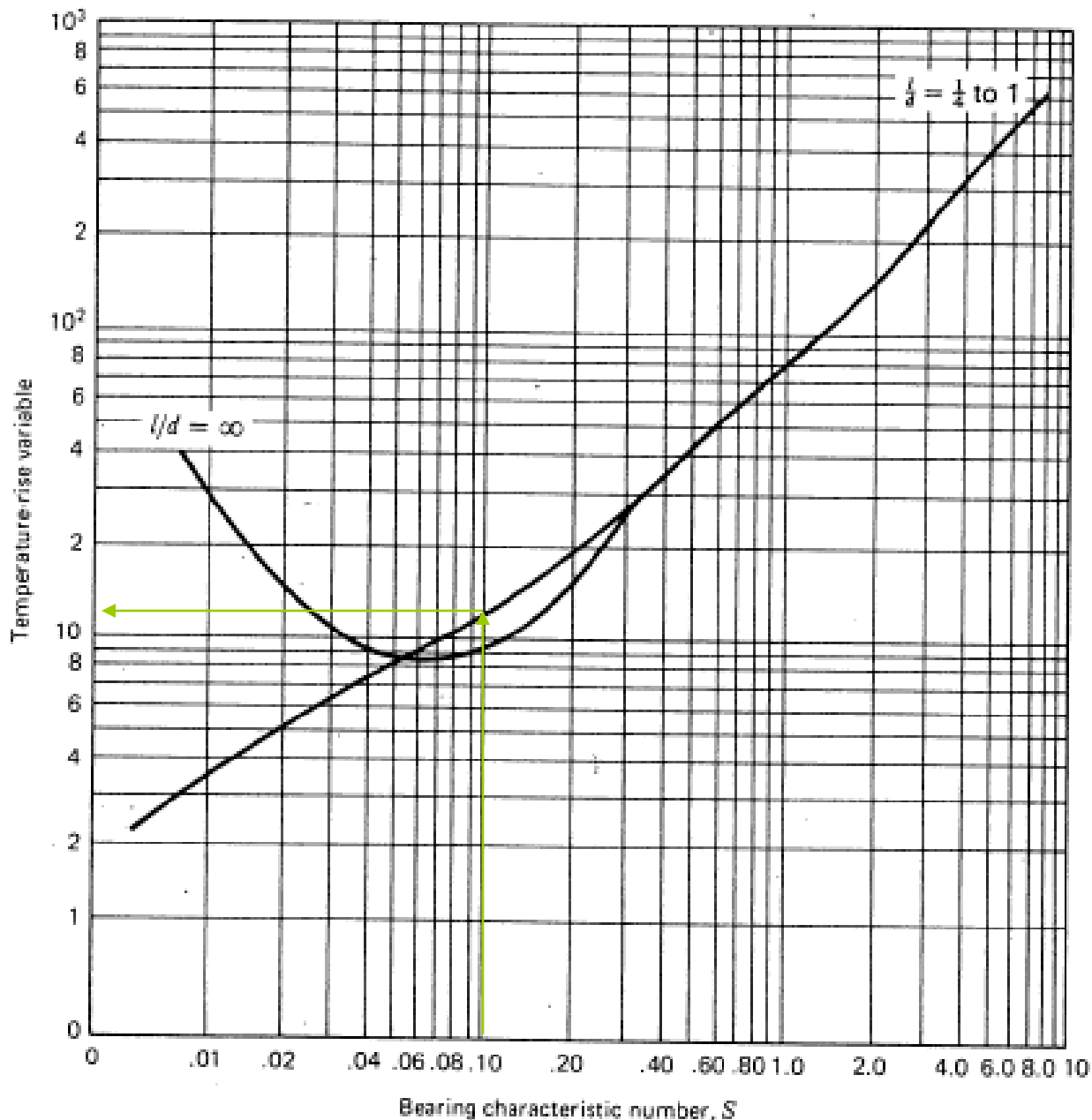


c)

$$\Delta T_{oc} = \frac{8.30 \times P}{\left[1 - \frac{1}{2} \times \frac{Q_s}{Q}\right]} \times \frac{\frac{r}{c} f}{\frac{Q}{rcNl}} = \frac{8.30 \times 0.6}{1 - \frac{1}{2} \times 0.87} \times \frac{3.535}{5.4} = 5.77 \text{ } ^\circ\text{C}$$

$$\theta_{P_{\max}} = 16.5^\circ \quad \frac{P}{P_{\max}} = 0.27 \quad P_{\max} = \frac{0.6}{0.27} = 2.22 \text{ MPa}$$





Based on eqn.

$$\Delta T_{oc} = T_{var} \frac{P}{\gamma C_H}$$

$$S=0.1, \quad l/d=1/2$$

$$T_{var}=14$$

$$P=0.6 \text{ MPa}$$

$$861 \text{ kg/m}^3$$

$$1760 \text{ J/kg-C}$$

$$\Delta T_{oc} = 14 * \frac{P}{\gamma C_H} = 5.5$$

FIGURE 12-12 Chart for temperature-rise variable $T(\text{var}) = \gamma C_H \Delta T/P$. In plotting this chart it was found that the curves for $l/d = \frac{1}{4}$, $\frac{1}{2}$, and 1 were so close together that they could not be distinguished from a single curve.

Example 6:

A journal which is turned and operates in bored and reamed cast bronze bearing has a diameter of 50 mm and a length of 25 mm.

The speed of journal is 1200 rpm. If SAE 20 oil of an inlet temperature of 45 °C is used for optimum (minimum) power loss.

Determine:

- a) The temperature rise of the oil
- b) The maximum load that can be supported by this bearing.
- c) Total oil flow and the side flow.
- d) The coefficient of friction.
- e) The maximum oil pressure and its angular location.
- f) The terminating position of the oil film.

Solution:

Turned journal

Bored and reamed cost bronze bearing

$d=50$ mm $l=25$ mm $\rightarrow l/d= 1/2$

$N= 1200$ rpm = 20 rps

SAE 20 oil $T_i=45$ ° C

$T=?$

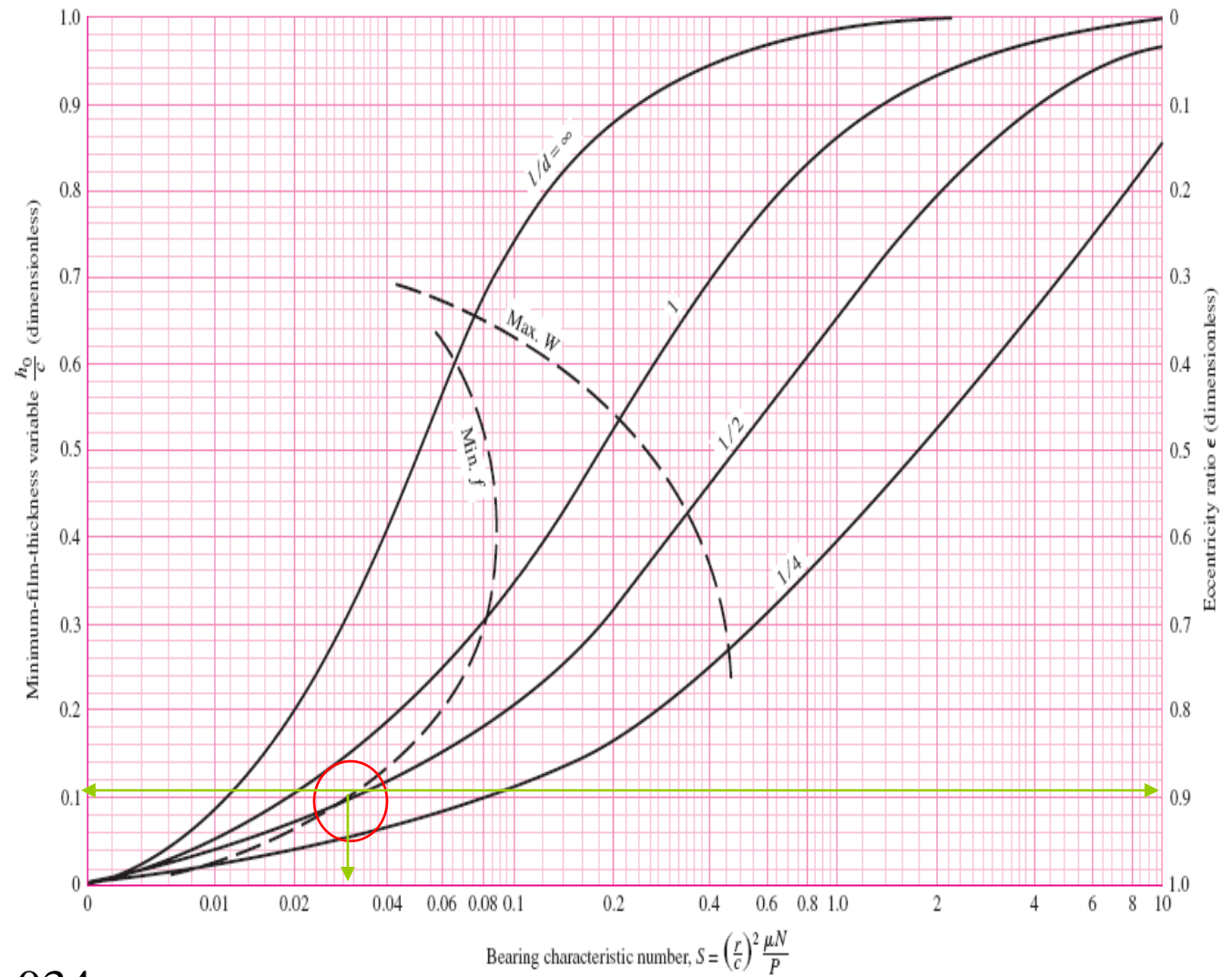
$W=?$

$Q?, Q_s?$

$f=?$

etc

From the graph for minimum power loss



For $\frac{l}{d} = \frac{1}{2}$

$\frac{h_0}{c} = 0.11$ and $S = 0.034$

a) From the graph for minimum power loss

$$\text{For } \frac{l}{d} = \frac{1}{2}$$

$$\frac{h_0}{c} = 0.11 \quad \text{and} \quad S = 0.034$$

$$\Delta T_{oc} = \frac{8.30 \times P}{\left[1 - \frac{1}{2} \times \frac{Q_s}{Q}\right]} \times \frac{\frac{r}{c} f}{\frac{Q}{rcNl}}$$

$$P = W/(ld) = ?,$$

$$W = ?$$

$$\text{or } \Delta T = T_{var} \frac{P}{\gamma C_H}$$

For $S = 0.034$

$$\frac{l}{d} = \frac{1}{2}$$

$$\frac{r}{c} f = 1.7 \quad \& \quad \frac{Q}{rcNl} = 5.65 \quad \& \quad \frac{Q_s}{Q} = 0.94$$

$$T_V = 7.$$

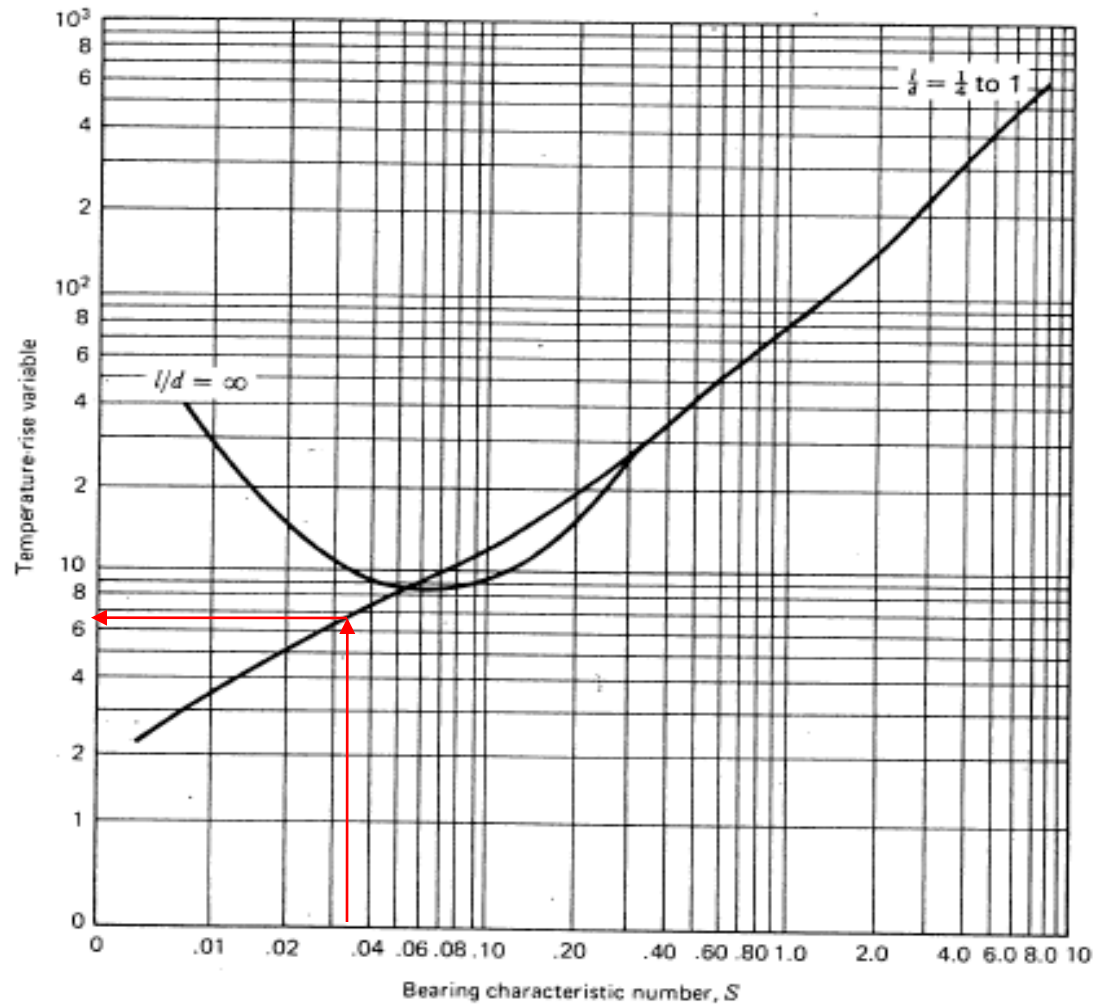
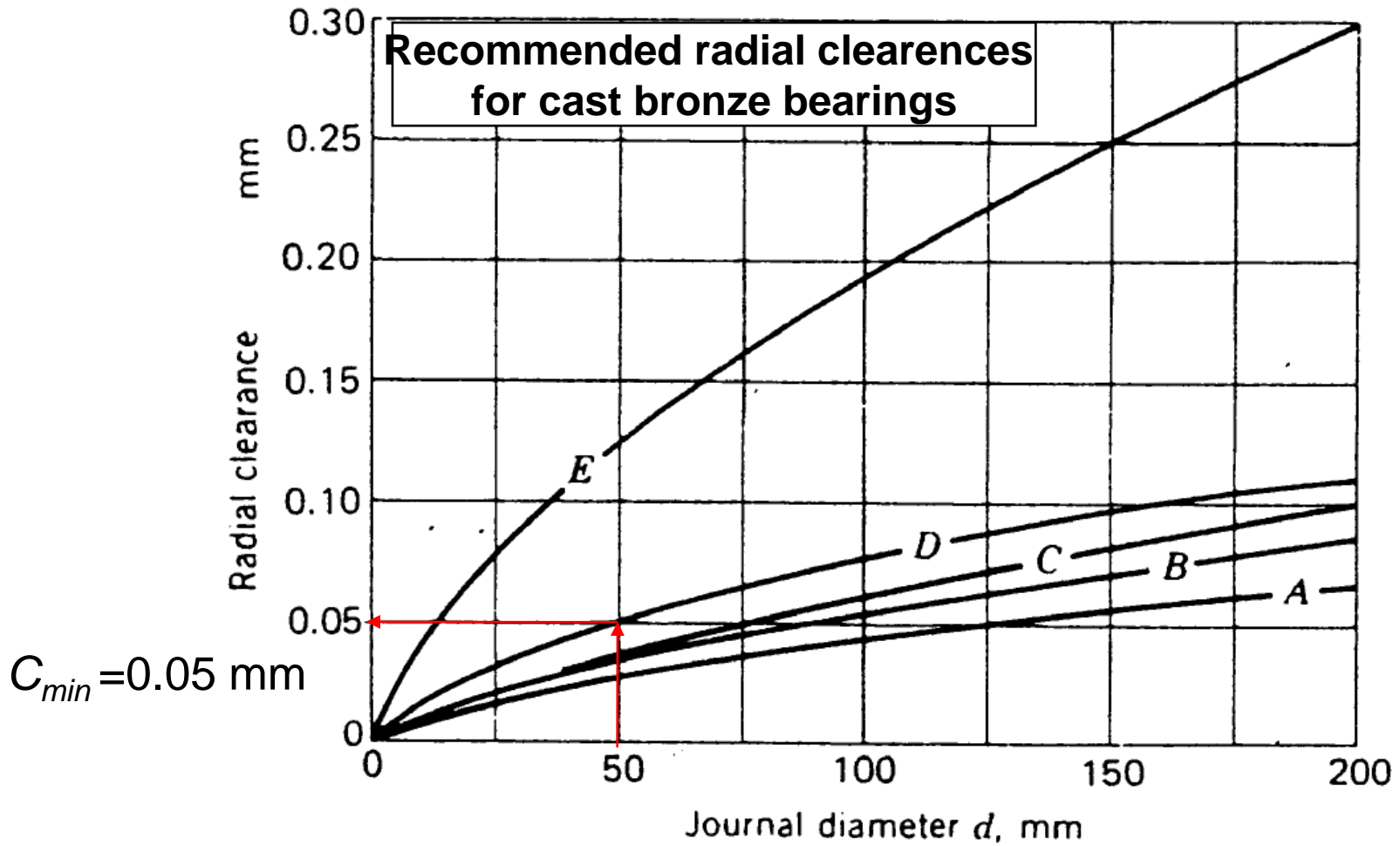


FIGURE 12-12 Chart for temperature-rise variable $T(\text{var}) = \gamma C_H \Delta T/P$. In plotting this chart it was found that the curves for $l/d = \frac{1}{4}$, $\frac{1}{2}$, and 1 were so close together that they could not be distinguished from a single curve.



Since ΔT depends on P ;

$$\Delta T = T_{\text{var}} \frac{P}{\gamma C_H}$$

and also P depends on μ

$$P = \left(\frac{r}{c} \right)^2 \frac{\mu N}{S}$$

and μ depends on ΔT

$$T_{\text{ave}} = T_{\text{in}} + \frac{\Delta T}{2}$$

we will use trial & error method for ΔT °C

$$\text{let } \Delta T = 16 \text{ } ^\circ\text{C} \rightarrow T_{\text{ave}} = 45 + \frac{16}{2} = 53 \text{ } ^\circ\text{C} \rightarrow$$

$$\mu = 24 \times 10^{-3} \text{ Pa-sec for SEA 20 oil}$$

$$\text{Then } P = \left(\frac{50/2}{0.05} \right)^2 \frac{24 \times 10^{-3} \times 20}{0.034} = 3.525 \text{ MPa}$$

$$\Delta T_{\text{ } ^\circ\text{C}} = T_{\text{var}} \frac{P}{\gamma C_H} = 7 \times \frac{3.525 \times 10^6}{861 \times 1760} = 16.6 \text{ } ^\circ\text{C} \cong \text{assumed } \Delta T \text{ OK}$$

$$b) \quad W = ?, = P \times (l \times d) = 3.525 \times 10^6 \times (0.025 \times 0.05)$$

$$W = 4406 \text{ N}$$

$$c) \quad Q = ? \quad \text{For } S = 0.34 \quad \frac{Q}{rcNl} = 5.65 \rightarrow Q = 5.65 \times 25 \times 0.05 \times 20 \times 50 = 3528 \text{ mm}^3 / \text{sec}$$

$$Q_s = ? \quad \frac{l'}{d} = \frac{1}{2} \quad \frac{Q_s}{Q} = 0.94 \rightarrow Q_s = 0.94 \times 3528 = 3317 \text{ mm}^3 / \text{sec}$$

$$d) \quad \frac{r}{c} f = 1.7 \quad \rightarrow \quad f = 1.7 \frac{0.05}{25} = 0.0034$$

$$e) \quad \frac{P}{P_{\max}} = 0.27 \quad \rightarrow \quad P_{\max} = \frac{P}{0.2} = \frac{3.525}{0.2} = 17.62 \text{ } \mu Pa \quad \theta_{P_{\max}} \cong 12^\circ$$

$$f) \quad \theta_{P_0} \cong 34^\circ$$

$$g) \quad h_0 = ? \quad \frac{h_0}{c} = 0.11 \rightarrow h_0 = 0.11 \times 0.05 = 0.0055 \text{ mm} \quad \underline{\underline{h_0 = 5.5 \text{ } \mu m}}$$

